

# Modeling of X-ray spectroscopies

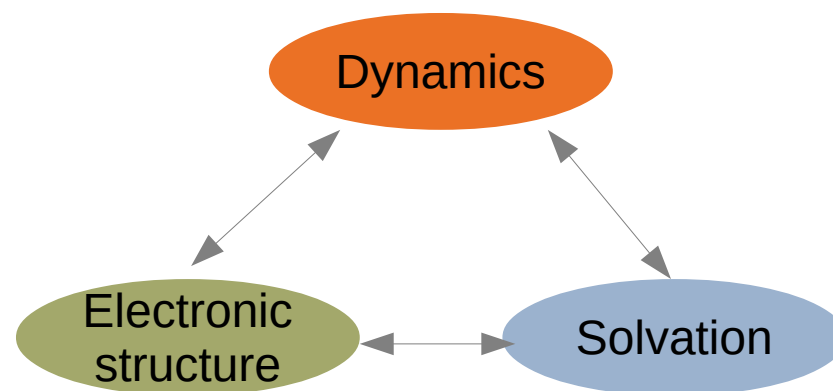
Michael Odelius  
Department of Physics

4FUTURE Intensive course 2019:  
Methods for Image and Spectral Data Analysis and Interpretation



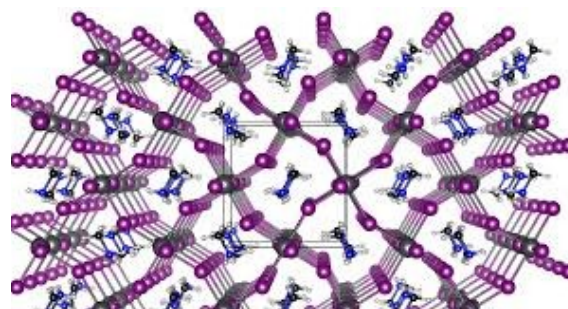
Stockholm  
University

# Ultrafast dynamics in solution



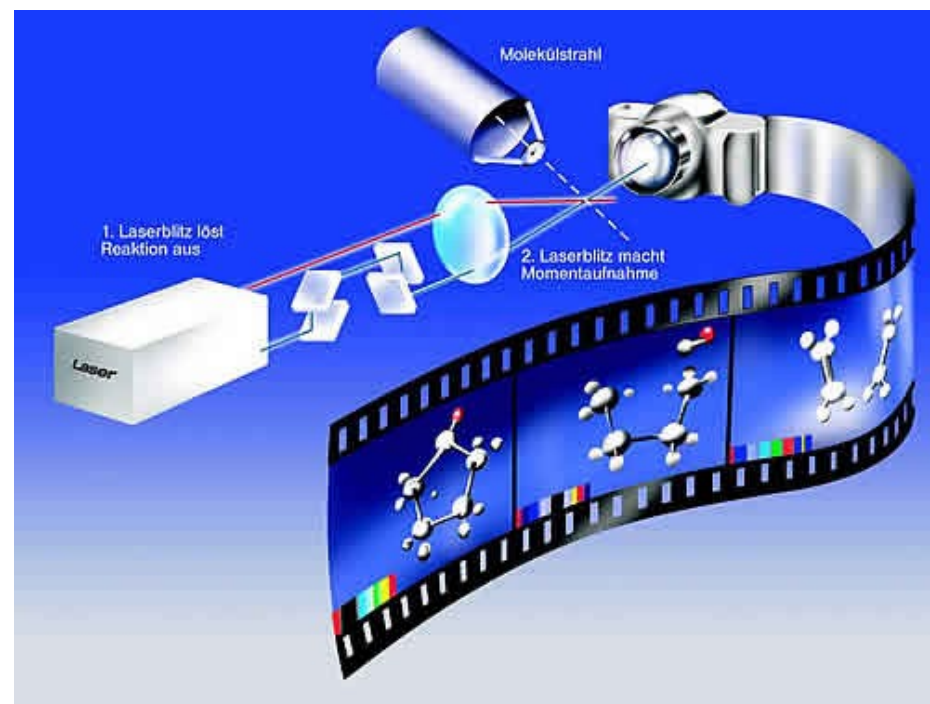
## Solar cell materials

**Hybridperovskites:  
Methylammonium  
leadtriiodide**



**Great photovoltaic properties, but  
environmental hazards and instability**

# Theoretical spectrum simulations - Why bother?



**Femtochemistry:** "Filming" chemical reactions using ultra-fast lasers.  
(Source: DESY Hamburg)

# Theoretical spectrum simulations - Why bother?

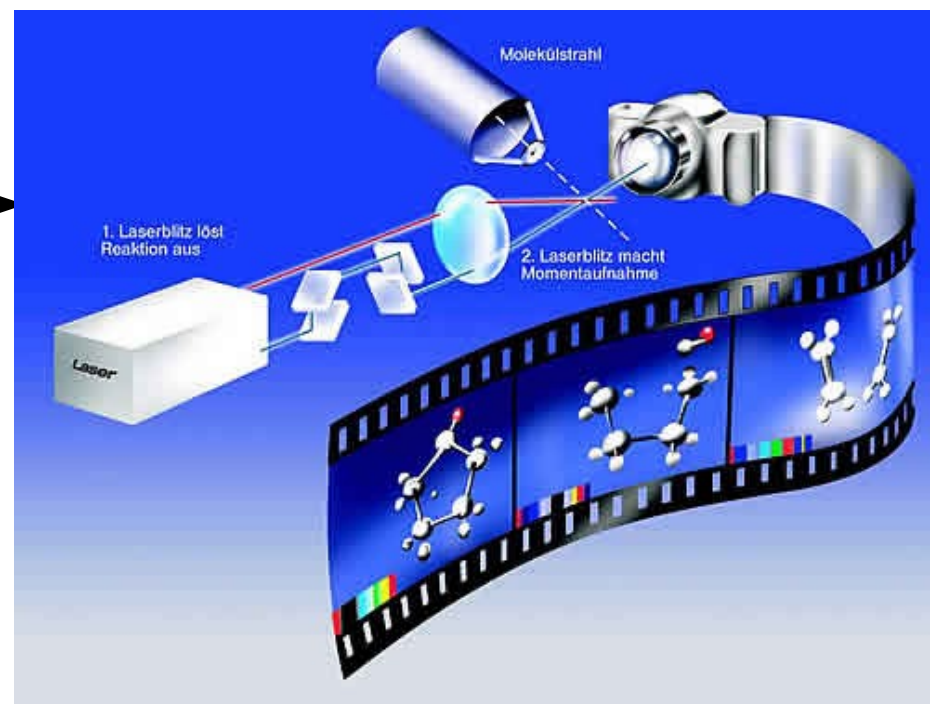
**Theory is required  
to develop the film**

**Qualitative  
assignment**

**Quantitative  
analysis**

**Evaluate  
theo. models**

**Evaluate  
approximations**



**Femtochemistry:** "Filming" chemical reactions using ultra-fast lasers.  
(Source: DESY Hamburg)

# Outline

## **Spectrum simulations – Part I**

**Molecular orbital approach**

## **Spectrum simulations – Part II**

**Electronic states approach**

**Dynamical effects**

**Excited state X-ray spectra**

# Core-level spectroscopy

**X-ray photo-electron spectroscopy**

**Core-ionization  
(Valence-ionization)**

**X-ray absorption spectroscopy**

**Core-excitation**

**X-ray emission spectroscopy**

**Fluorescence decay**

**Resonant inelastic X-ray Scattering**

**Fluorescence decay**

**XPS XAS XES RIXS**

**Resonant photo-electron spectrosc.**

**Auger decay  
(dominate for small Z)**

# Quantum Chemistry $\mathcal{H}\Psi = E\Psi$

## Hartree-Fock

- 1) Born-Oppenheimer
- 2) Mean-field approx.

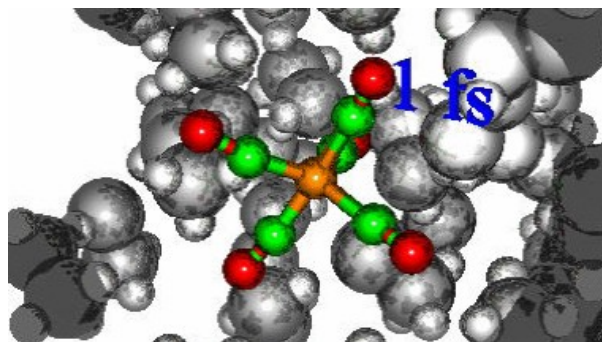
$$\Psi_{\text{HF}} = \det | \phi_1, \phi_2, \dots, \phi_N |$$

Momentary  
e<sup>-</sup> - e<sup>-</sup> correlation  
missing!

## DFT

Singlet determinant

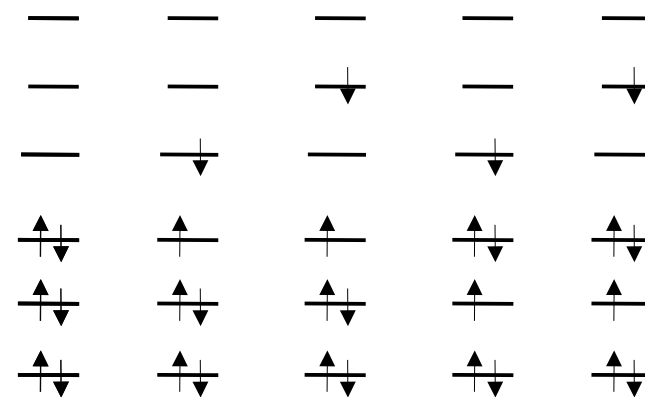
Correlation in  $\mathcal{H}$



## Post-HF

Multi-determinant

Wave function correlated



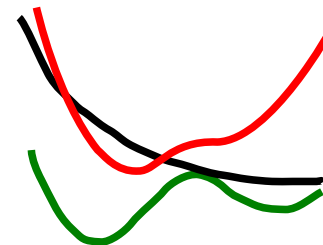
## Ab initio Molecular dynamics

$$F=ma$$

$$F_I = -\nabla_I \langle H_e \rangle \approx -\langle \Psi_0 | \nabla_I H_e | \Psi_0 \rangle$$

## Quantum dynamics

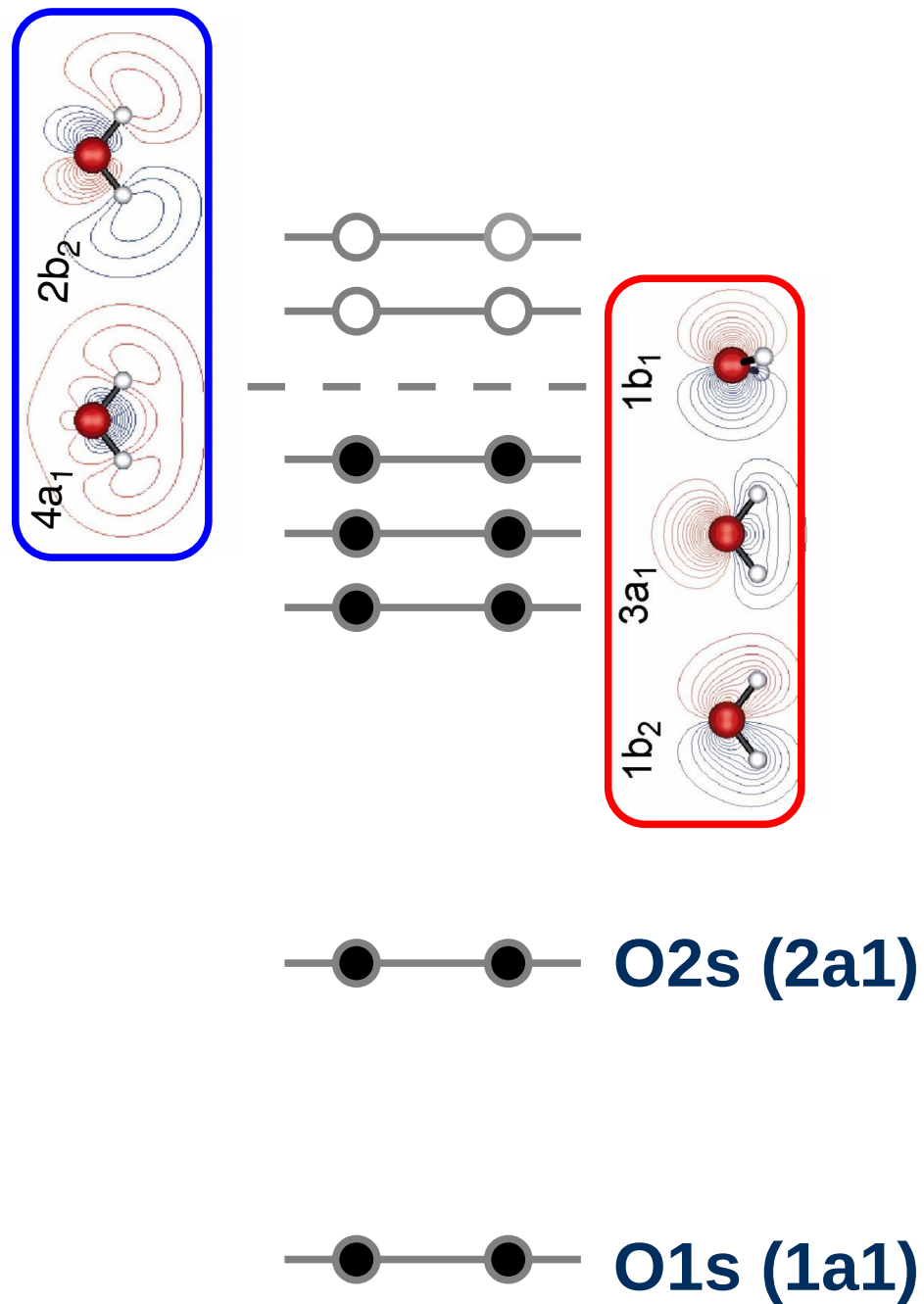
$$i\hbar \frac{\partial}{\partial t} \Phi(\{\mathbf{r}_i\}, \{\mathbf{R}_I\}; t) = H \Phi(\{\mathbf{r}_i\}, \{\mathbf{R}_I\}; t)$$



AIMD: CPMD Cp2k

QMD: Wave packet simulations

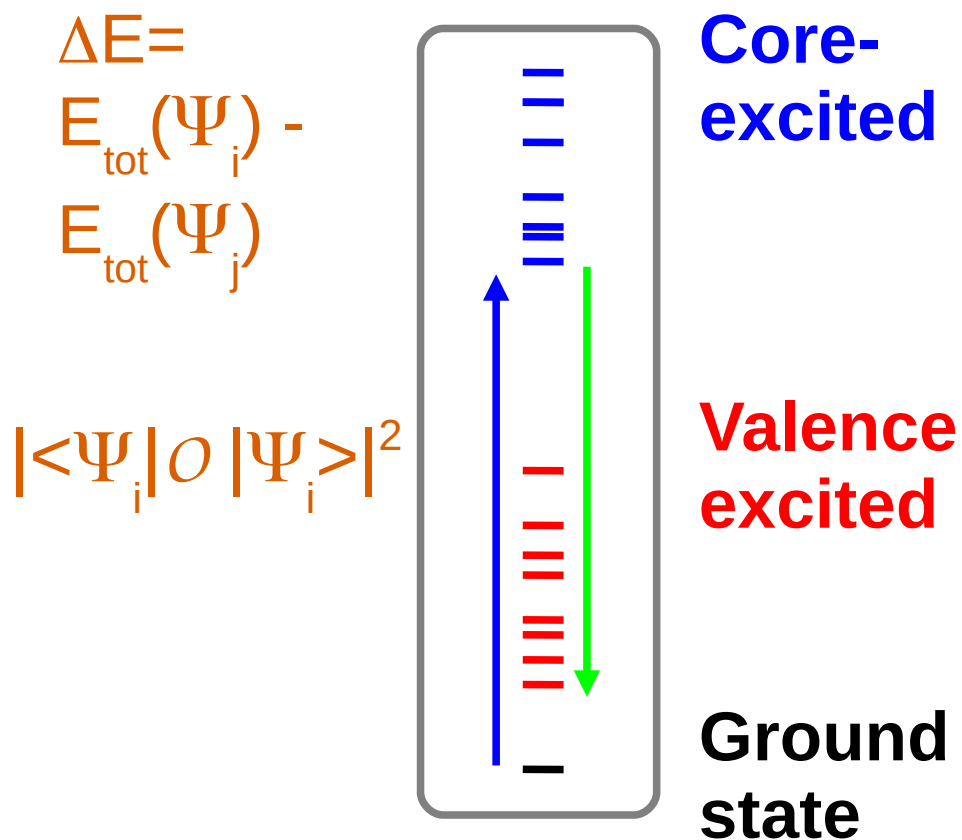
# Molecular orbitals of $\text{H}_2\text{O}(\text{g})$ - $\text{C}_{2v}$ Point group



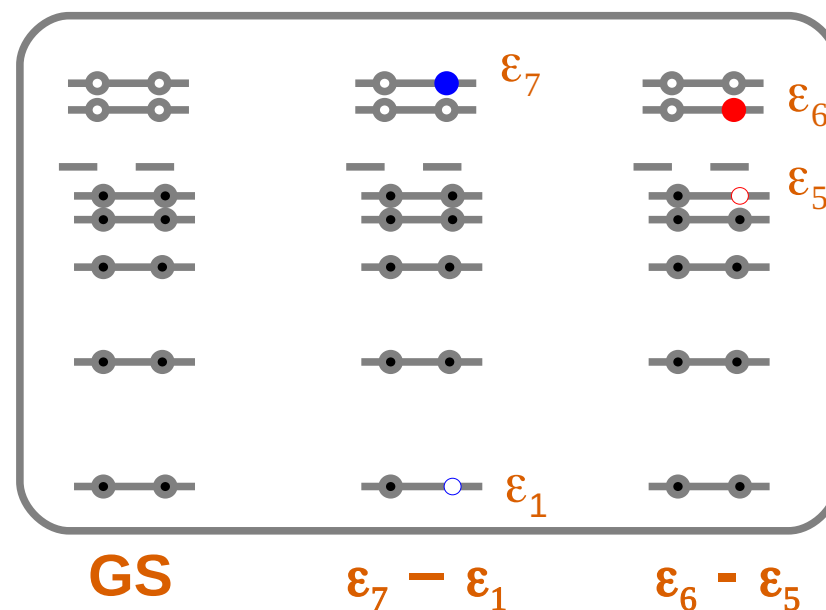


# Spectrum simulations $\mathcal{H}\Psi = E\Psi$

## Accurate methods Electronic states



## Approximate methods Molecular orbitals



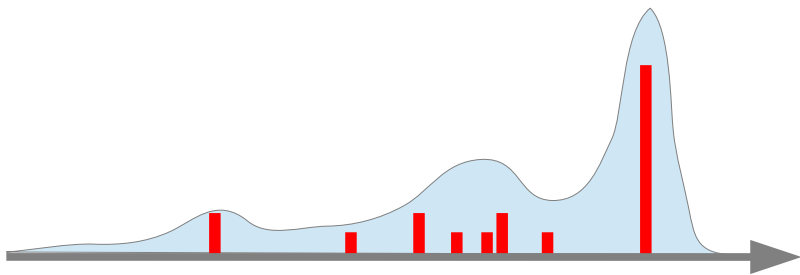
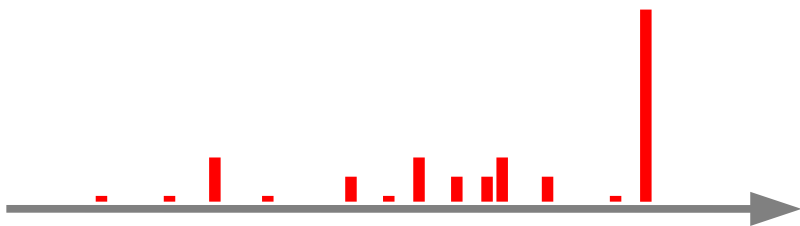
## Transition potential DFT

$$|\langle \Psi_i | O | \Psi_j \rangle|^2 = |\langle \phi_m | O | \phi_n \rangle|^2$$

# Spectrum simulations $\mathcal{H}\Psi = E\Psi$

$$E_{\text{tot}}(\Psi_i) - E_{\text{tot}}(\Psi_j)$$

$$|\langle \Psi_i | O | \Psi_j \rangle|^2$$



## Broadening:

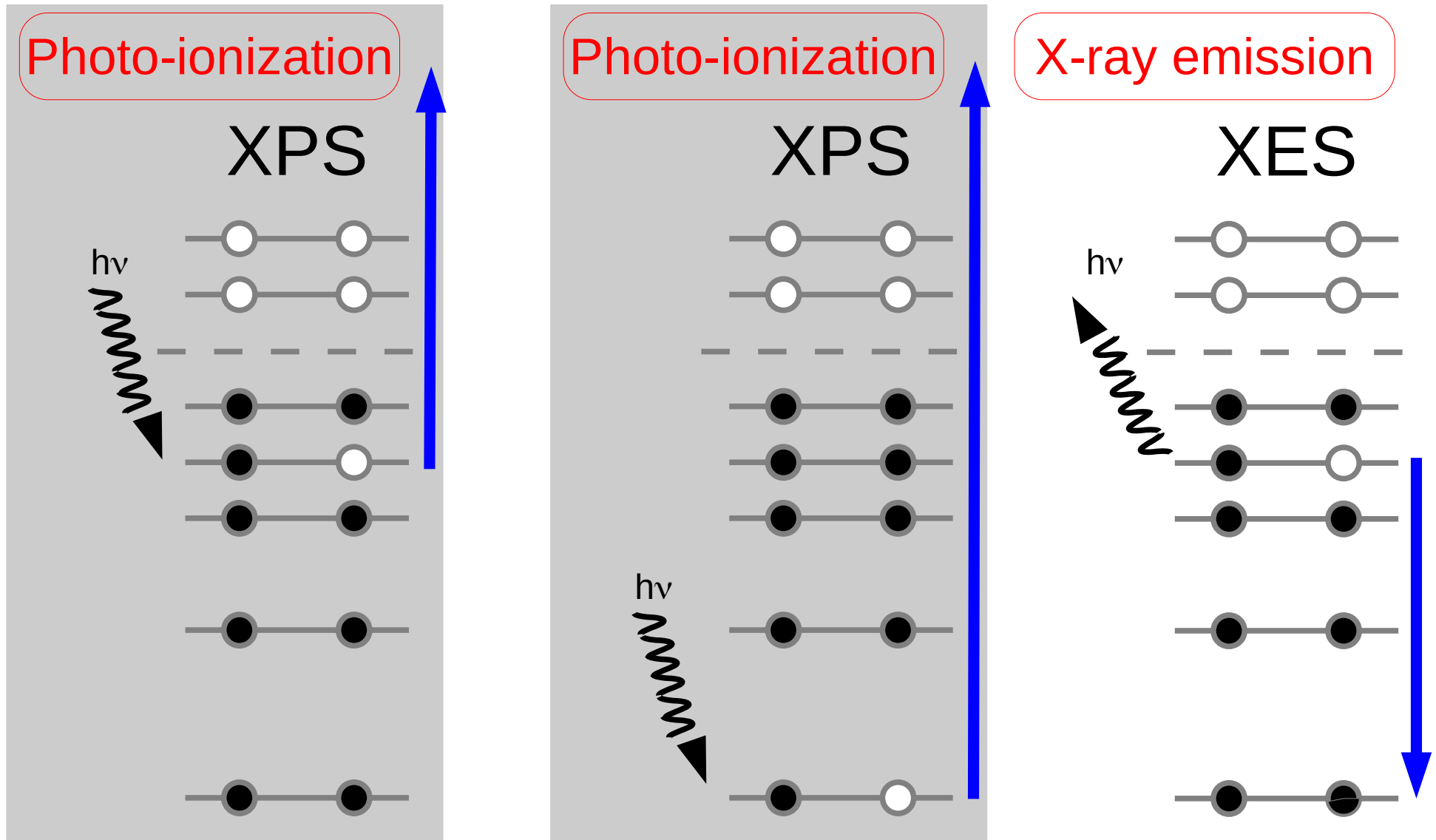
Core-hole life-time

Vibrational

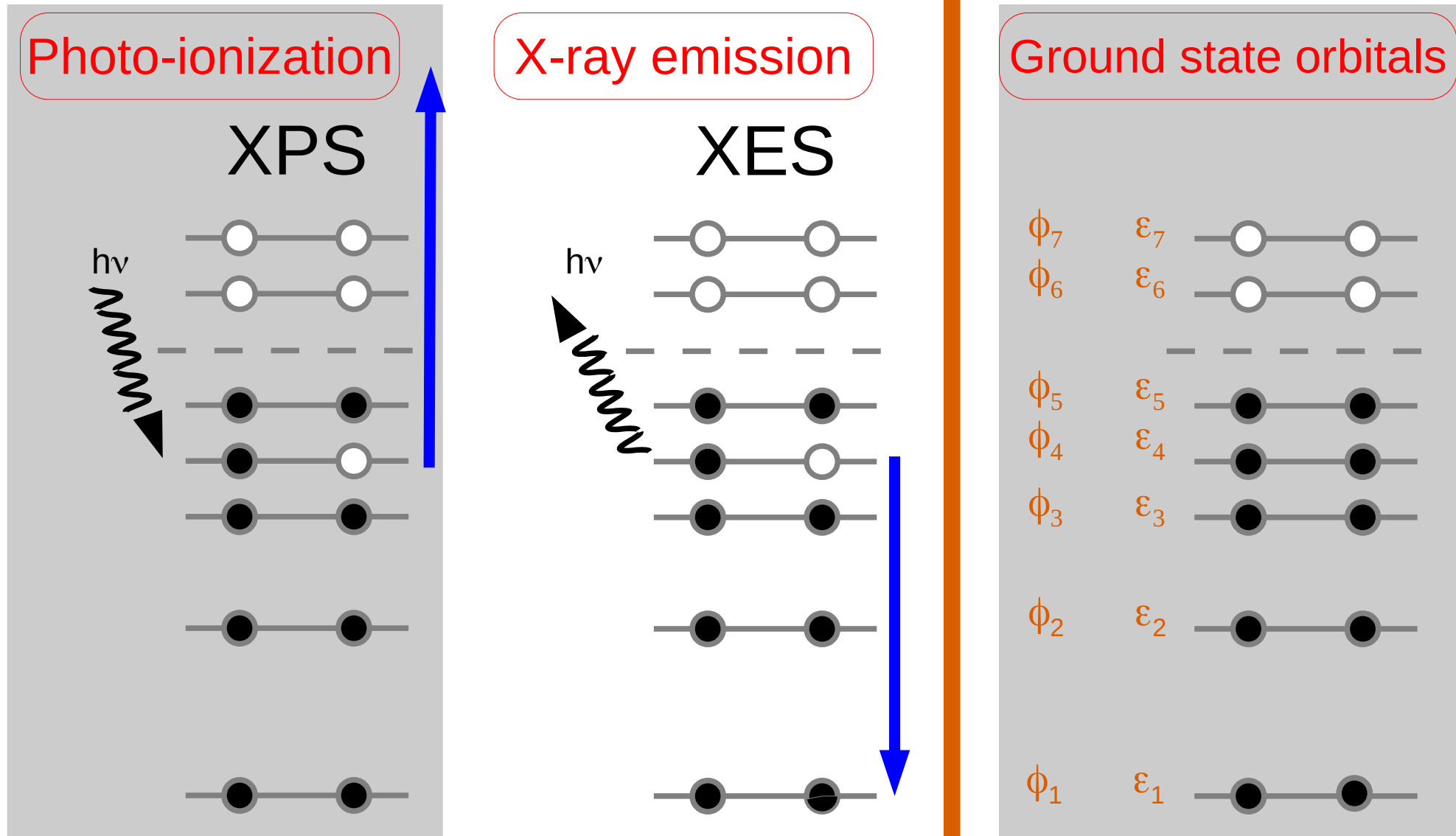
Configurational

Experimental

# Orbital representation of the XPS and XES processes



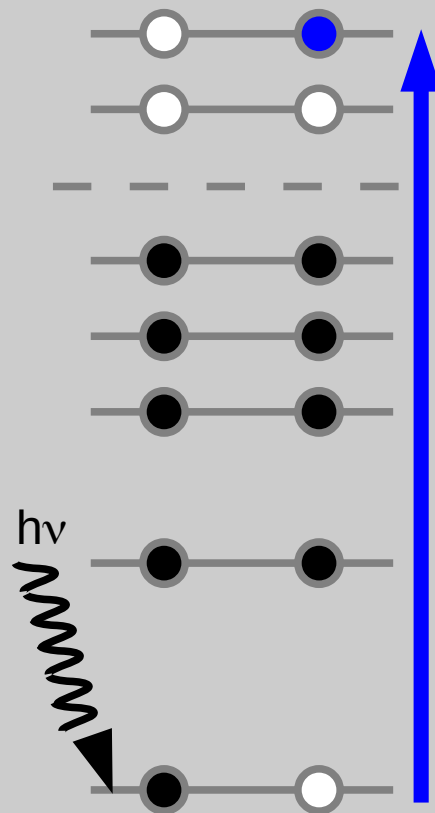
# Orbital representation of the XPS and XES processes



# Orbital representation of the XA process

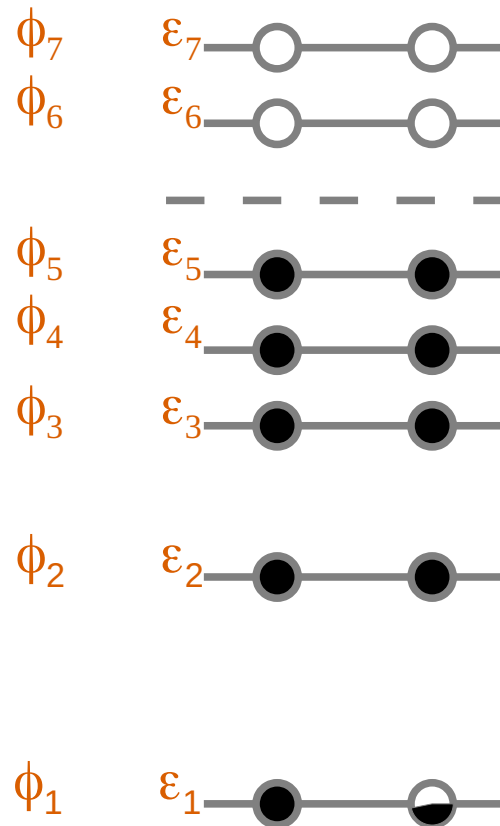
Xray absorption

XAS



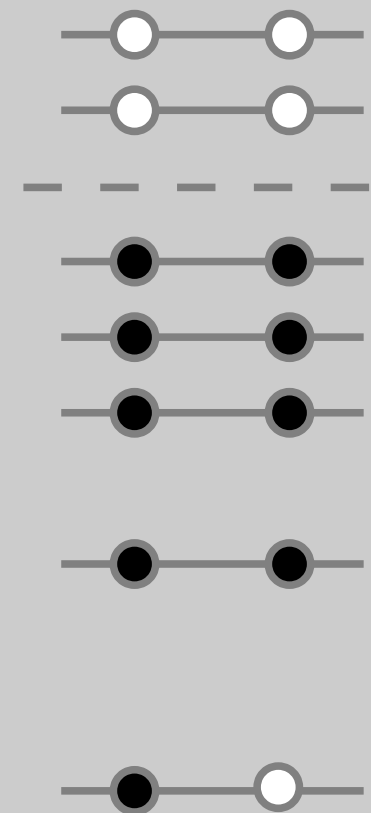
Half-core-hole

HH

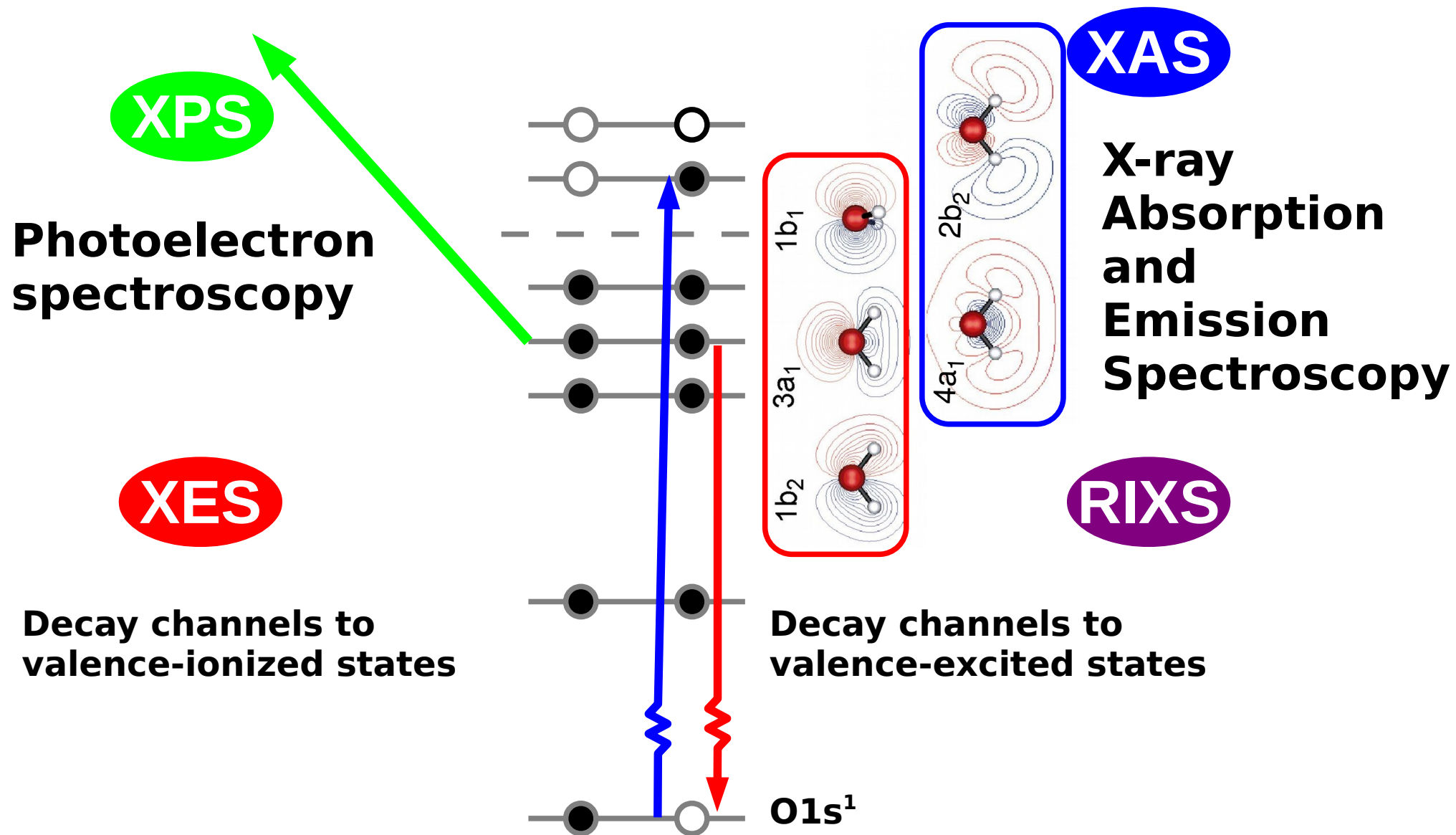


Full-core-hole

FH

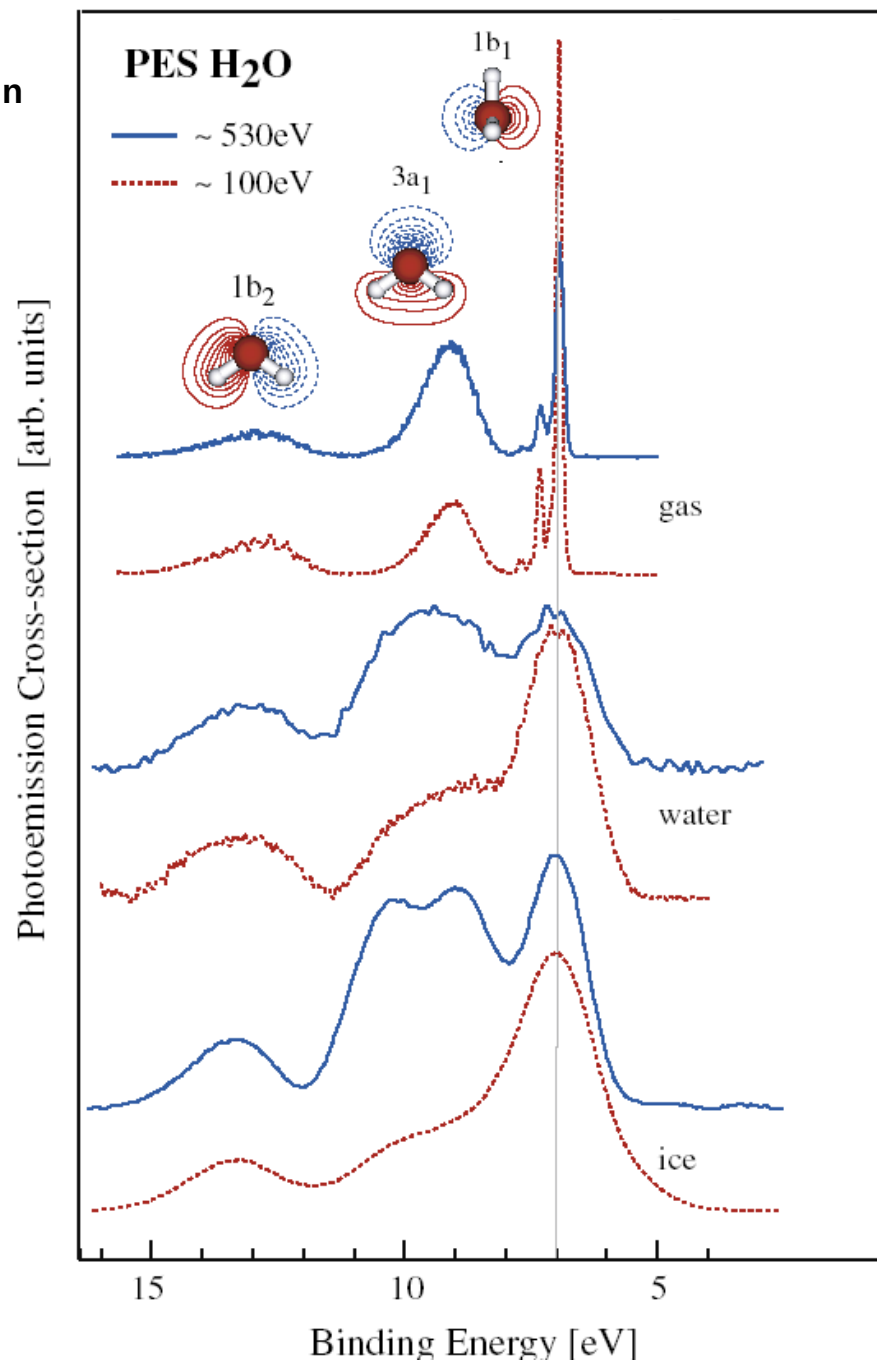


# X-ray spectroscopy Case study: H<sub>2</sub>O(g)



# Photo electron spectroscopy of $\text{H}_2\text{O}(\text{g},\text{l},\text{s})$

$$E_{\text{binding}} = E_{\text{photon}} - E_{\text{kin}}$$



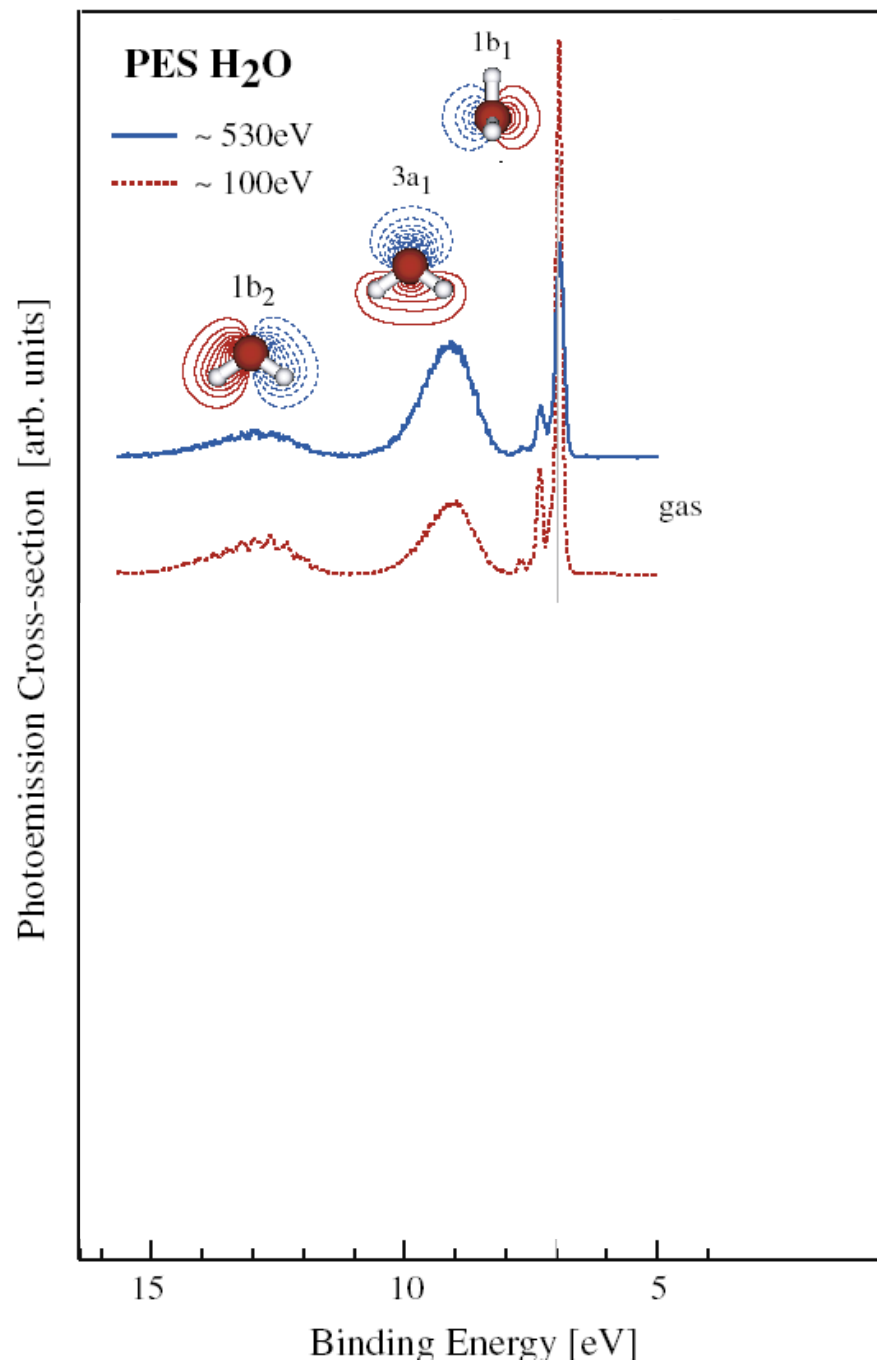
## Koopman's theorem

HF orbital energies  
 approximate

Ionization binding  
 energies

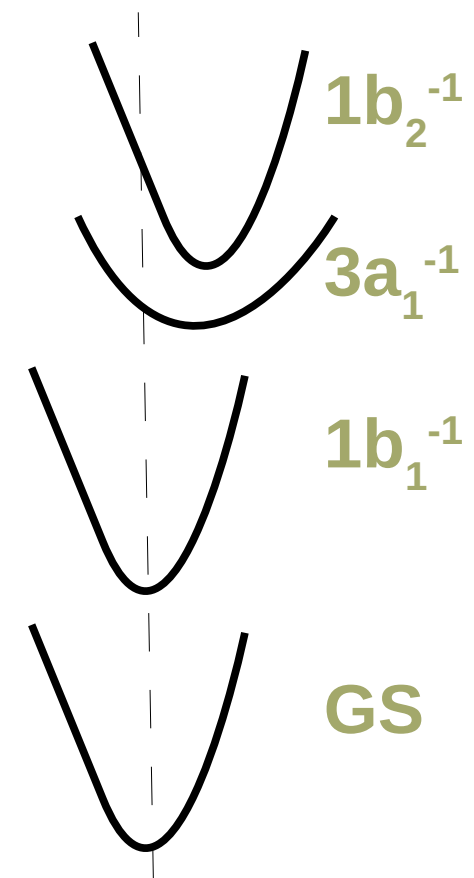
(However, we will  
 cheat and also use  
 DFT Kohn-Sham  
 energies which  
 require ad hoc shifts)

# Photo electron spectroscopy of $\text{H}_2\text{O}(\text{g},\text{l},\text{s})$



## Franck-Condon

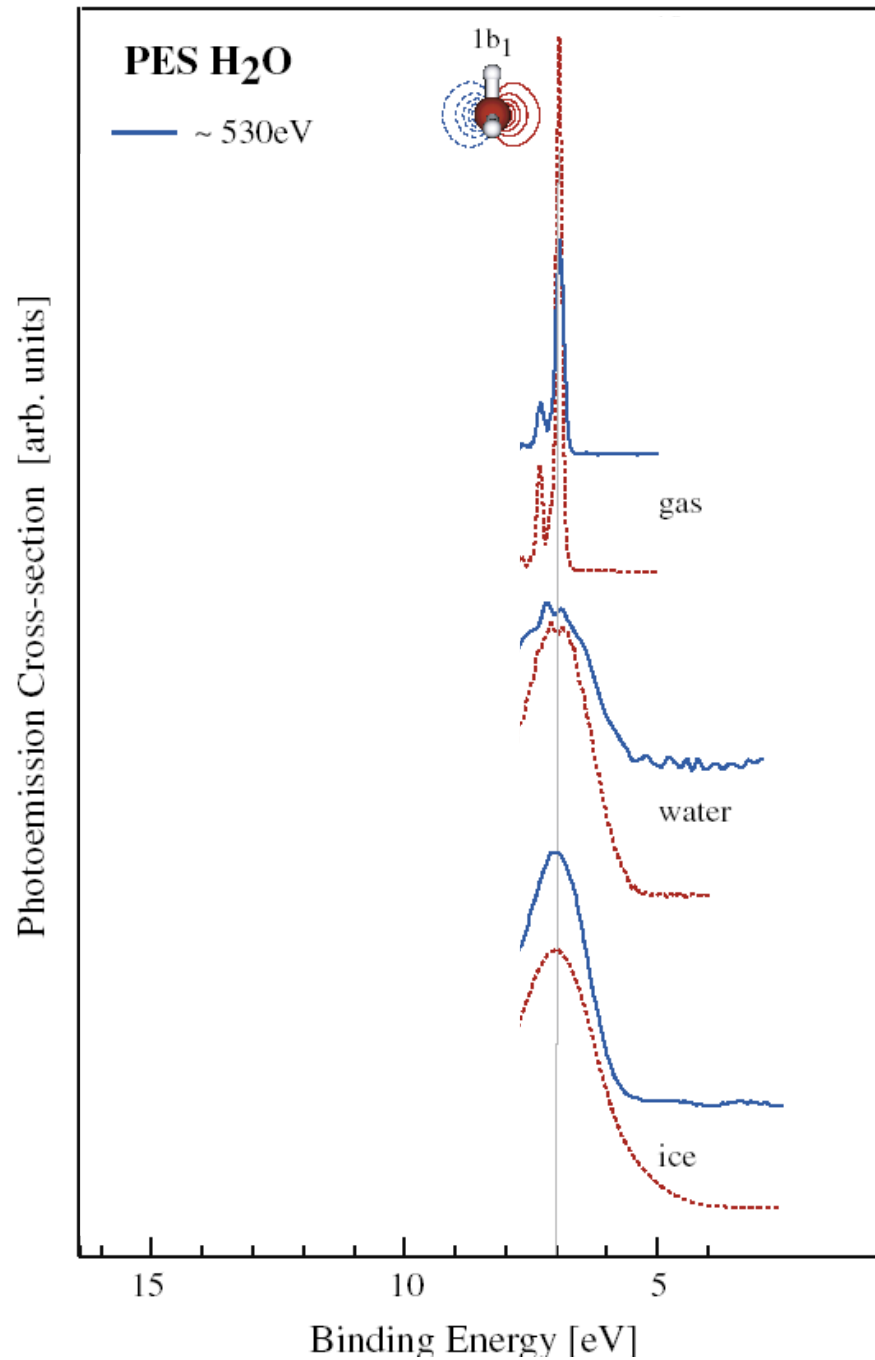
Vibrational excitations



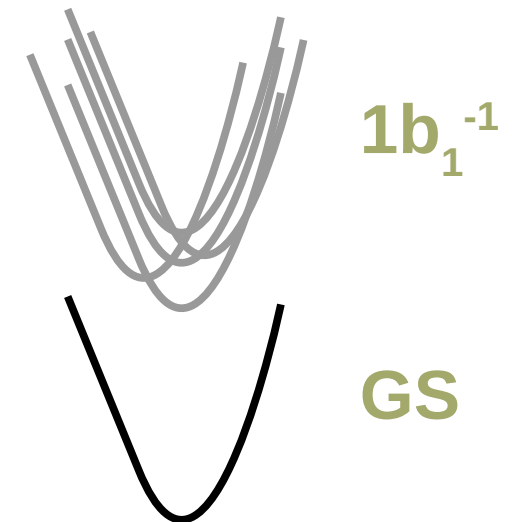
D. Nordlund et al  
 CPL **460** 86 (2008)



# Photo electron spectroscopy of $\text{H}_2\text{O}(\text{g},\text{l},\text{s})$



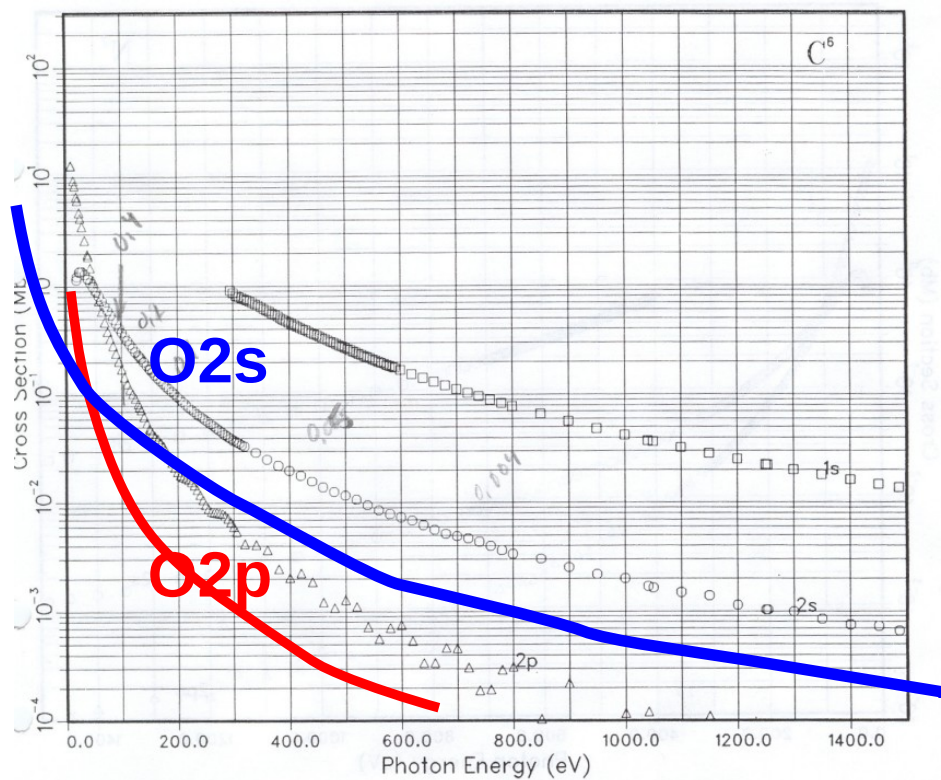
## Inhomogeneous Broadening



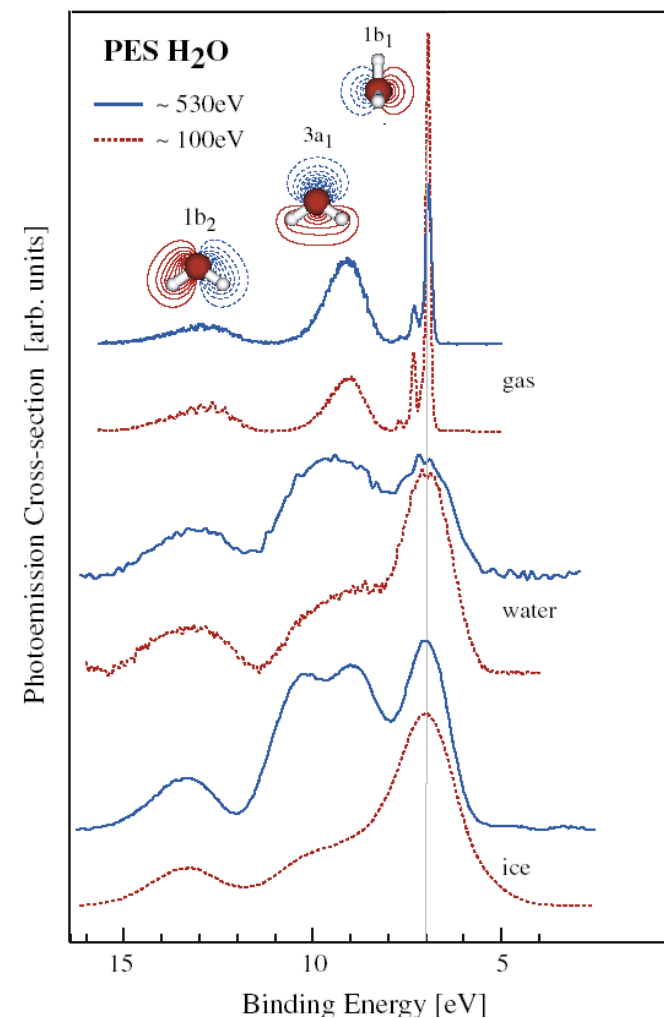
(Homogeneous broadening is due to finite life-times)

# Photo electron spectroscopy of $\text{H}_2\text{O}(\text{g},\text{l},\text{s})$

Cross-sections vary with photonenergy

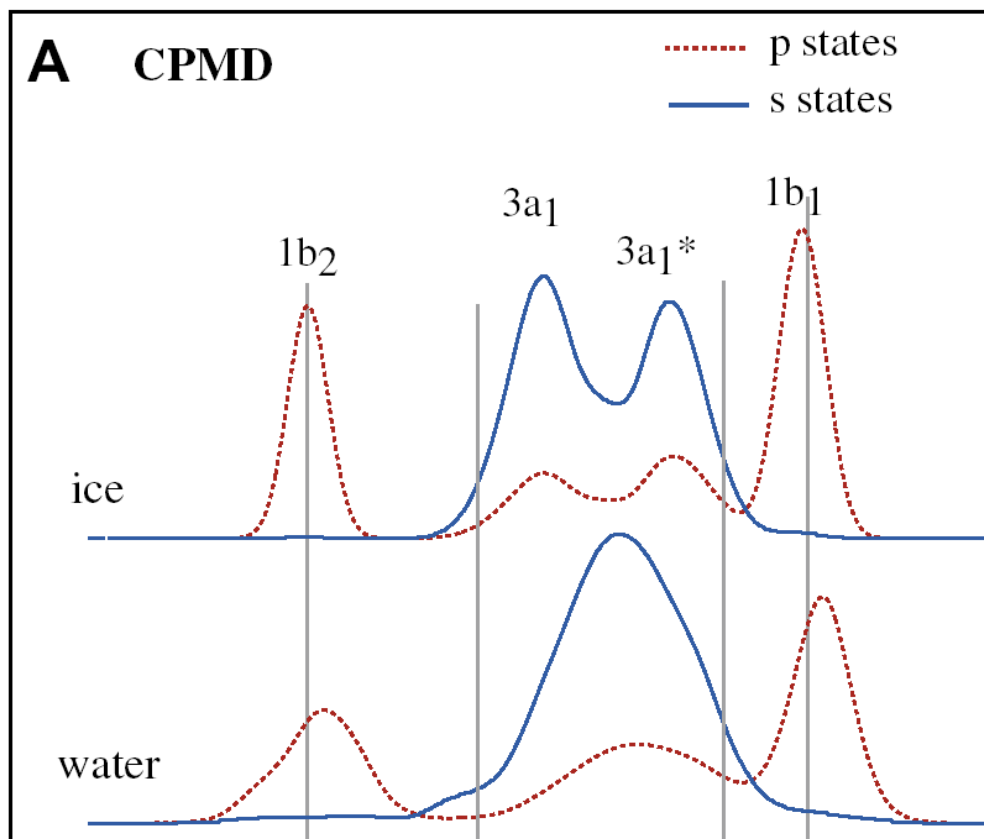


C binding energies(eV) are:  
 1s( 2) 290.860      2s( 2) 17.5409      2p( 2) 8.98202

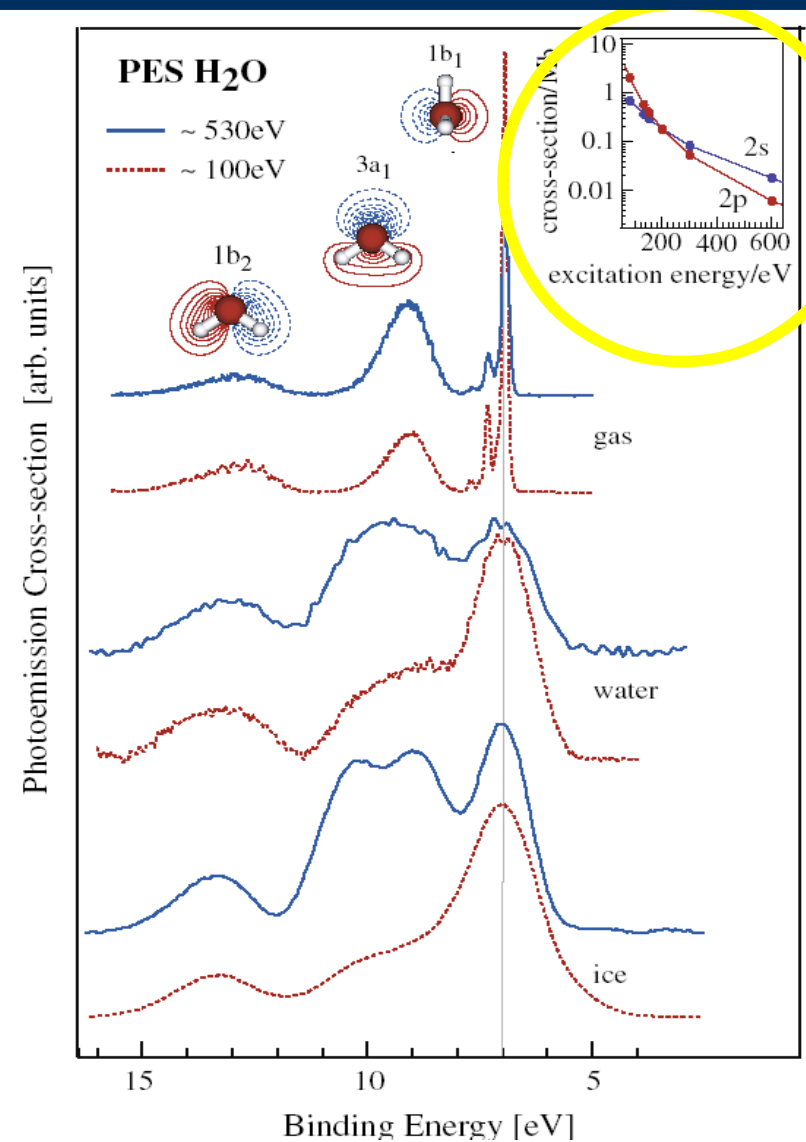


D. Nordlund et al  
 CPL **460** 86 (2008)

# Photo electron spectroscopy of H<sub>2</sub>O(l,s)

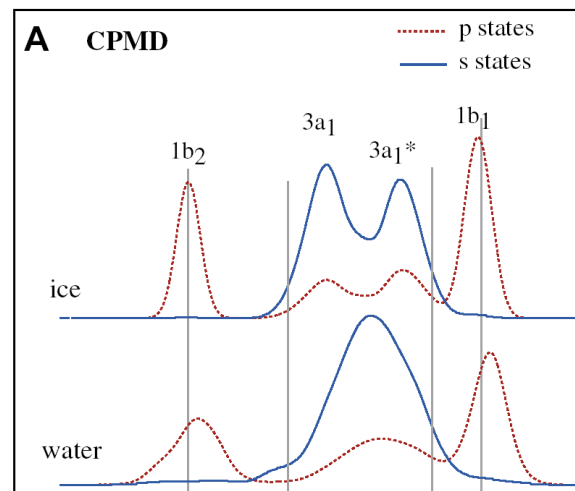
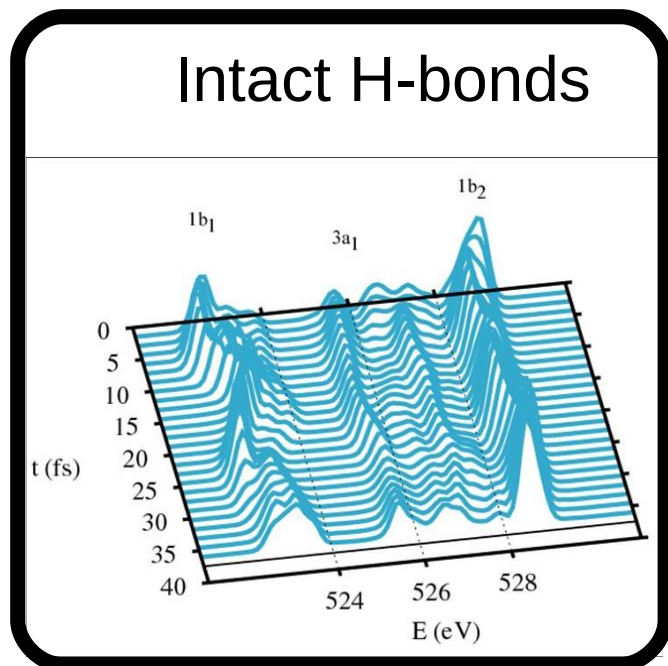


**Notice: In C<sub>2v</sub> symmetry only a<sub>1</sub> can have oxygen s-sym.**

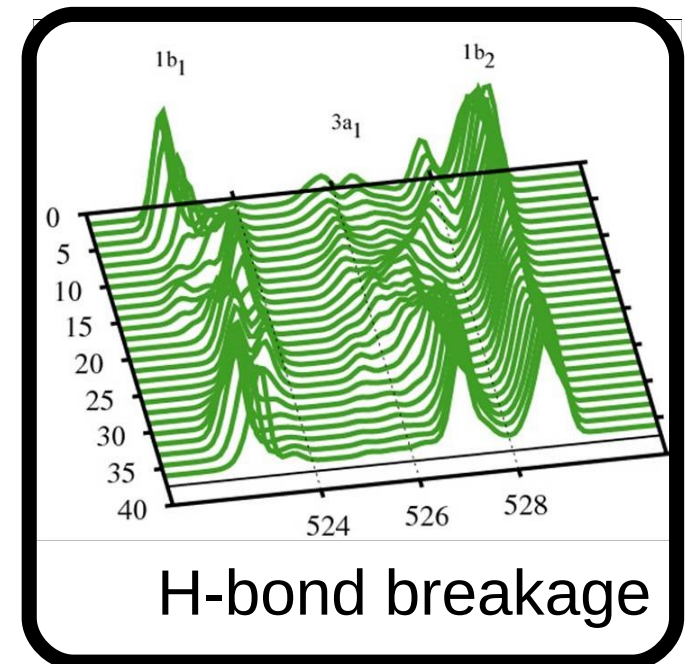


D. Nordlund et al  
CPL **460** 86 (2008)

## Time evolution of the electronic structure due to hydrogen bond dynamics

Hydrogen bond dynamics

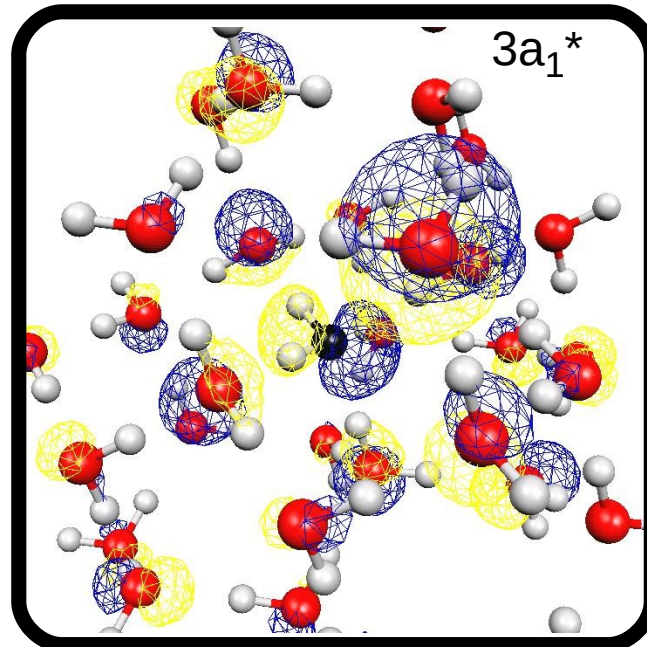
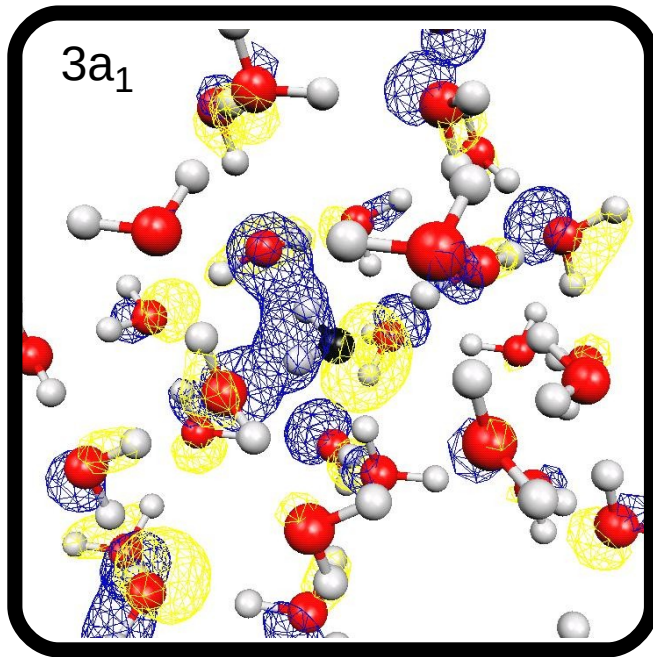
D. Nordlund et al  
CPL **460** 86 (2008)



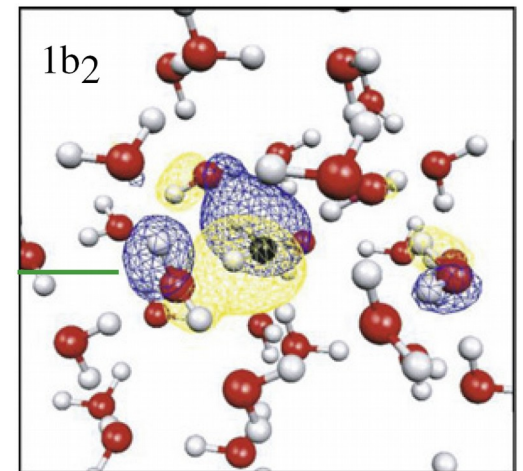
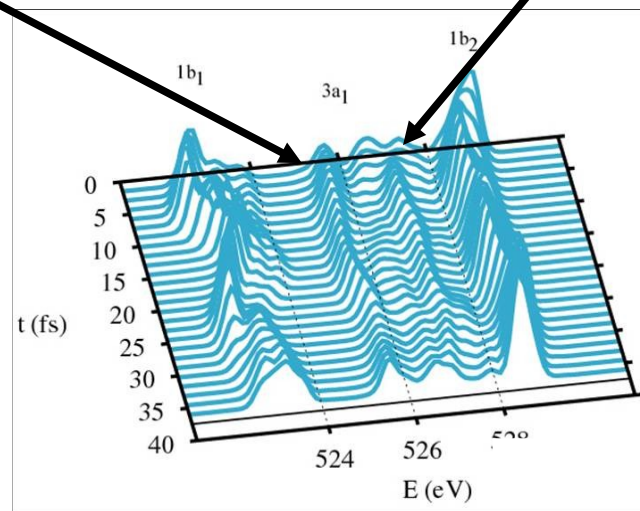
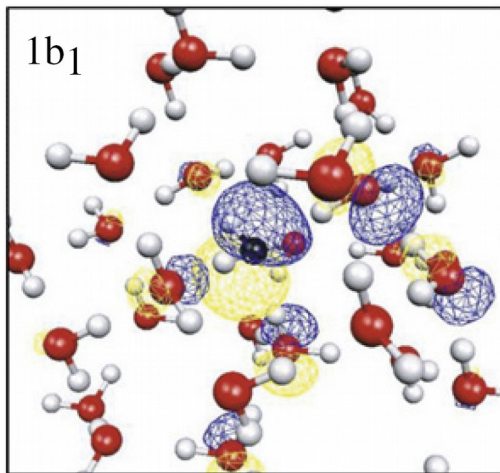
Car-Parrinello MD  
simulations



# Hydrogen bonding in water

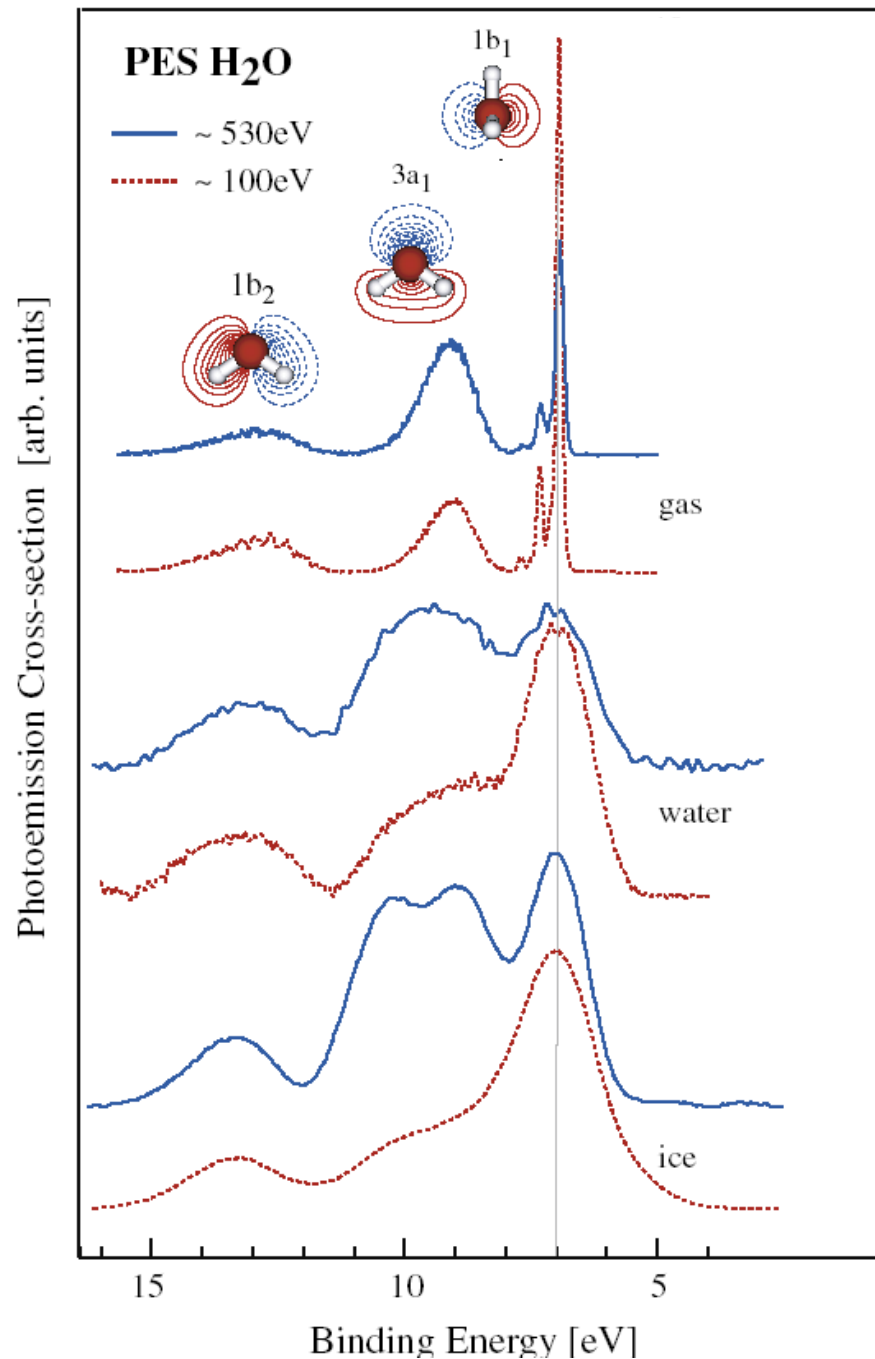


Strong  
overlap  
in  $3a_1$



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# Photo electron spectroscopy of $\text{H}_2\text{O}(\text{g},\text{l},\text{s})$



**Franck-Condon**

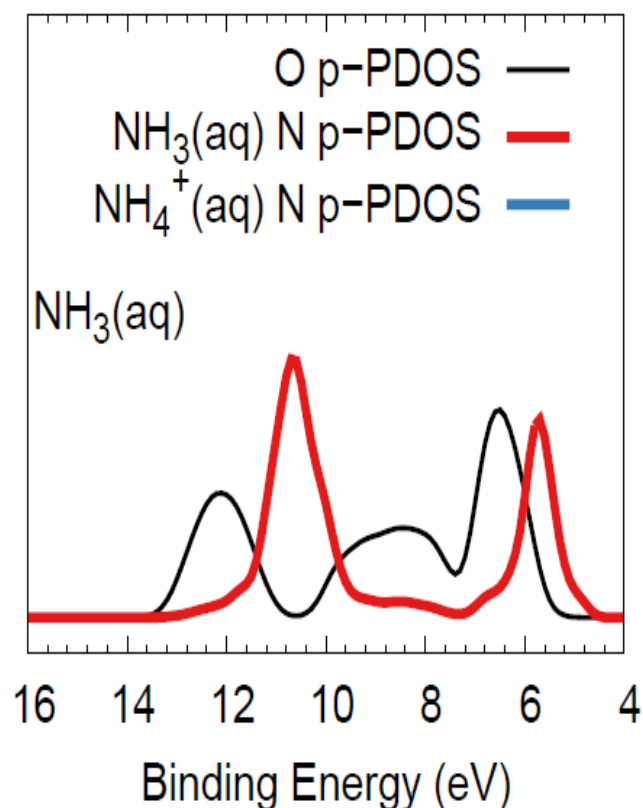
**Inhomogeneous broadening**

**Chemical bonding**

**Hydrogen bonding and dynamics**

# XES allows us to access N p-DPOS in $\text{NH}_3(\text{aq})$

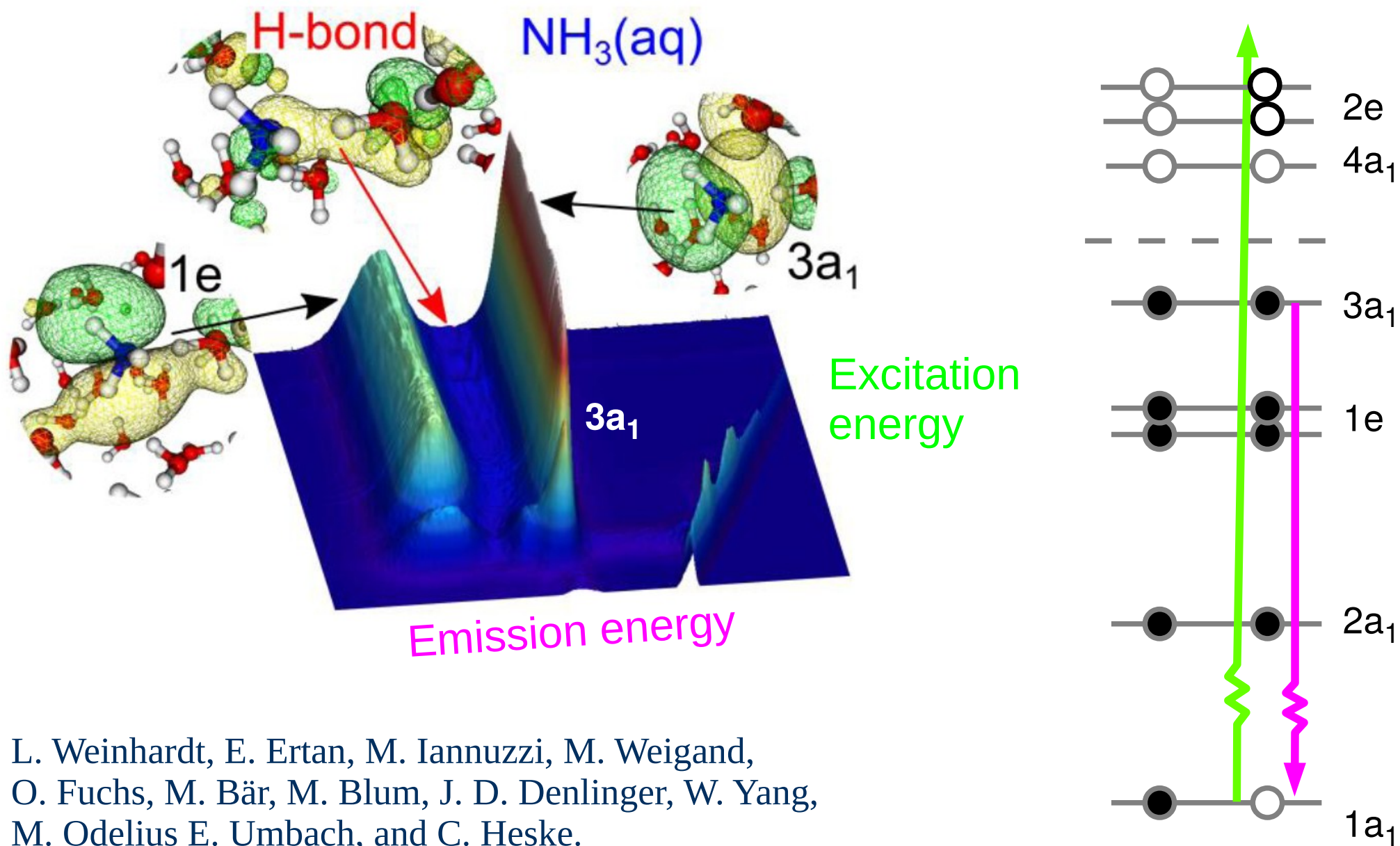
Aqueous ammonia:  
Energy mismatch in orbital mixing



**O PDOS would dominate in valence XPS**

**N K-edge XES can cut-out N p-PDOS**

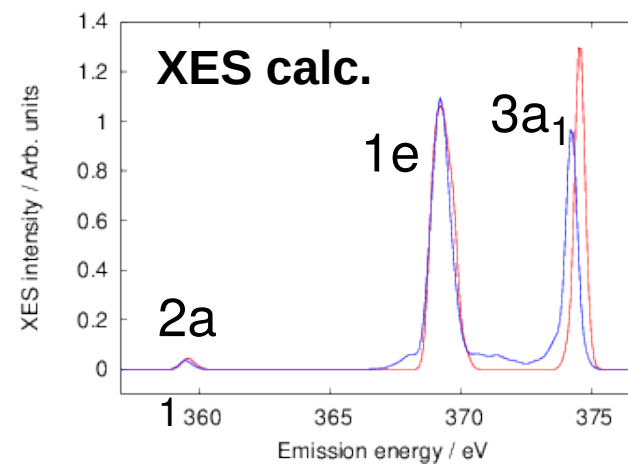
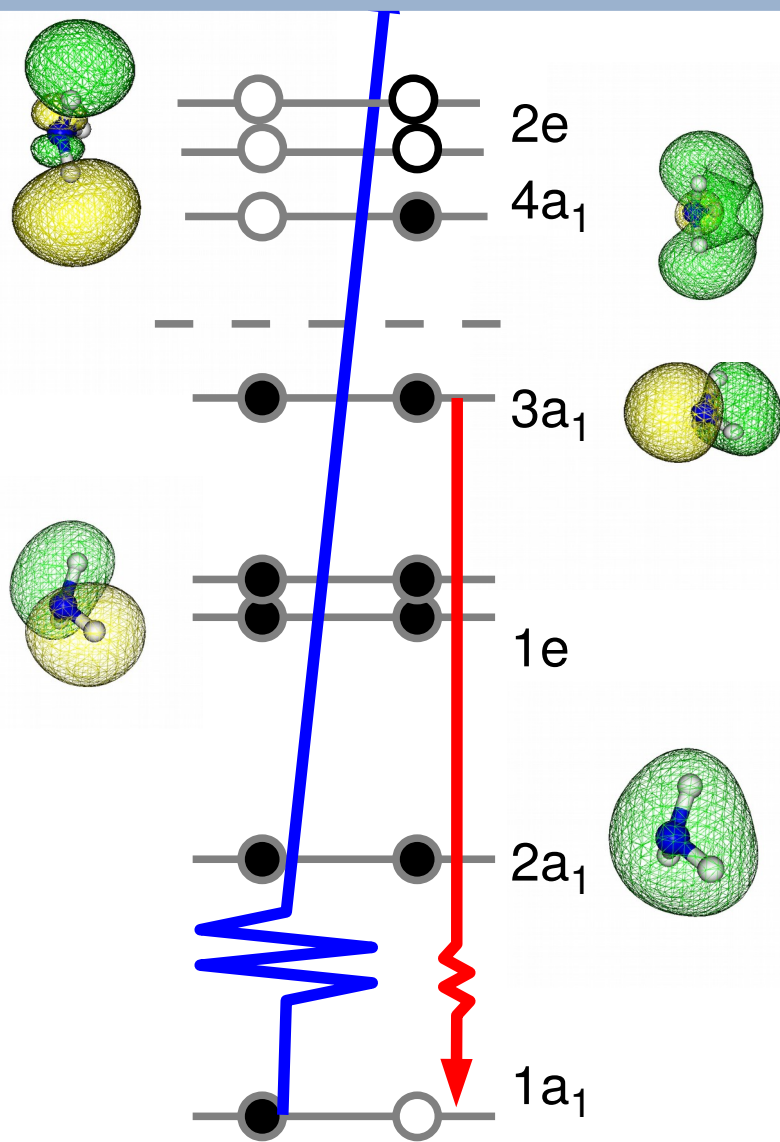
# X-ray emission spectroscopy of $\text{NH}_3(\text{g})$ and $\text{NH}_3(\text{aq})$



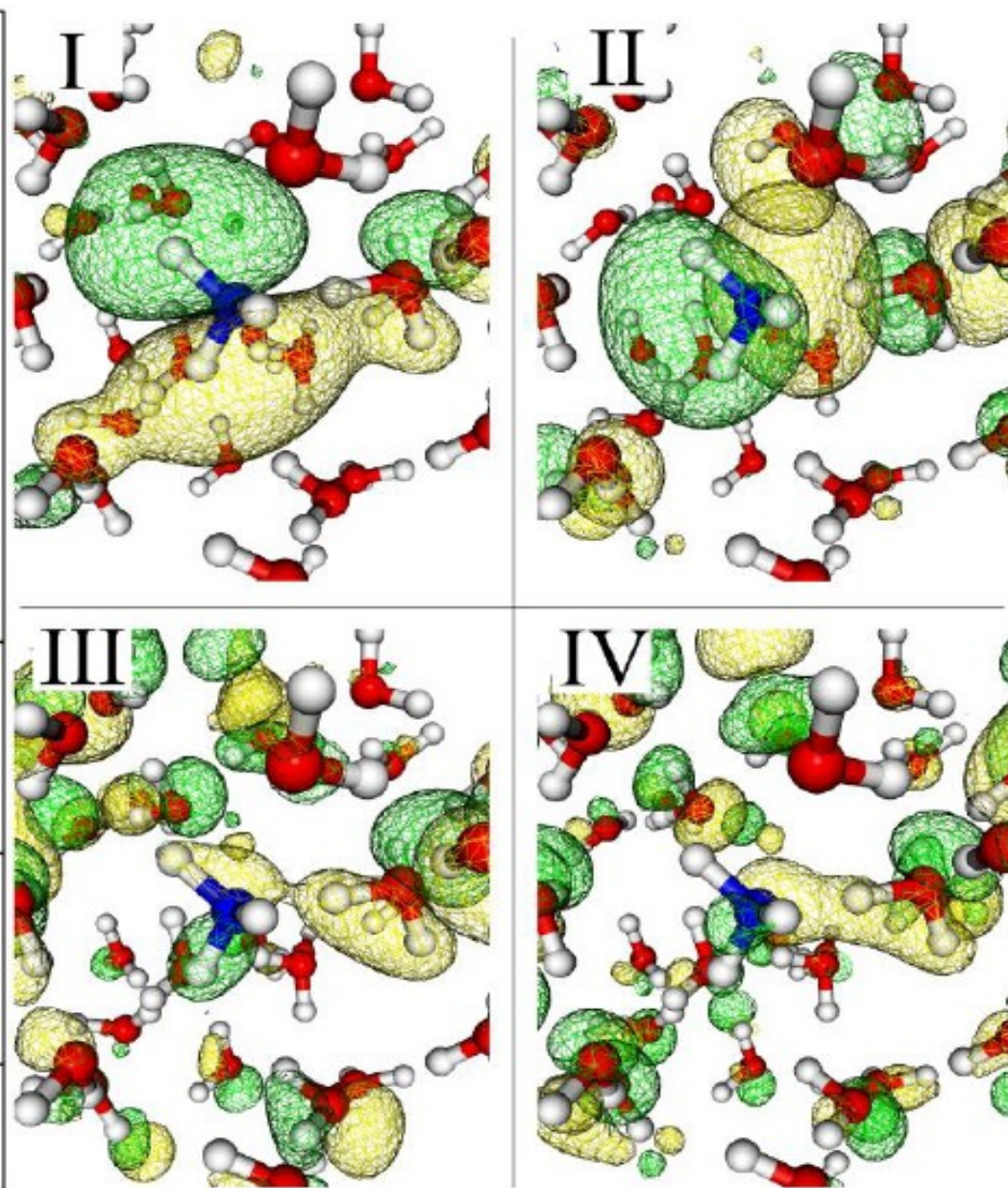
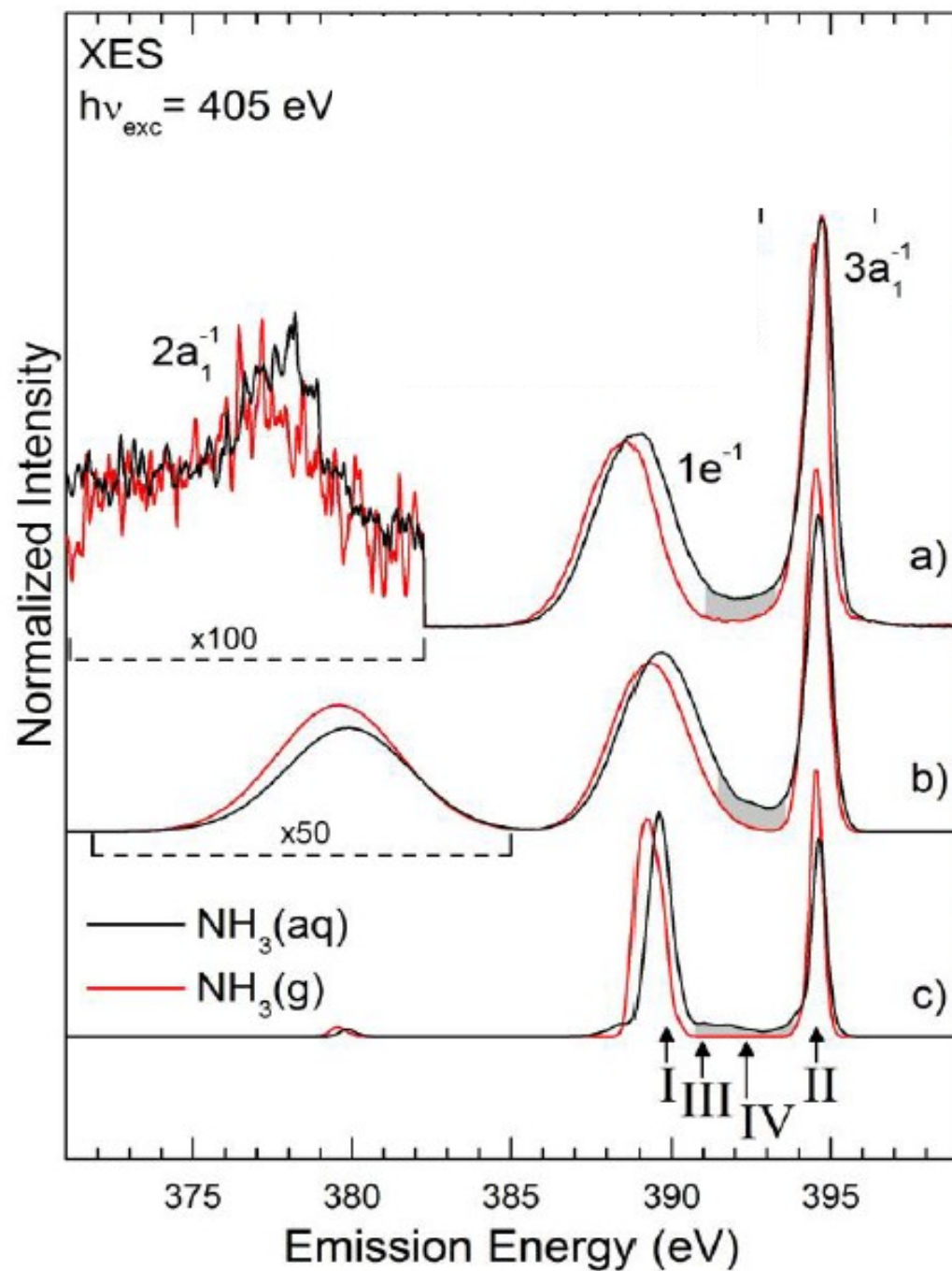
L. Weinhardt, E. Ertan, M. Iannuzzi, M. Weigand,  
 O. Fuchs, M. Bär, M. Blum, J. D. Denlinger, W. Yang,  
 M. Odelius E. Umbach, and C. Heske.  
 Phys. Chem. Chem.Phys., **17**, 27145 (2015)



# Electronic structure of $\text{NH}_3(\text{g})$ and $\text{NH}_3(\text{aq})$

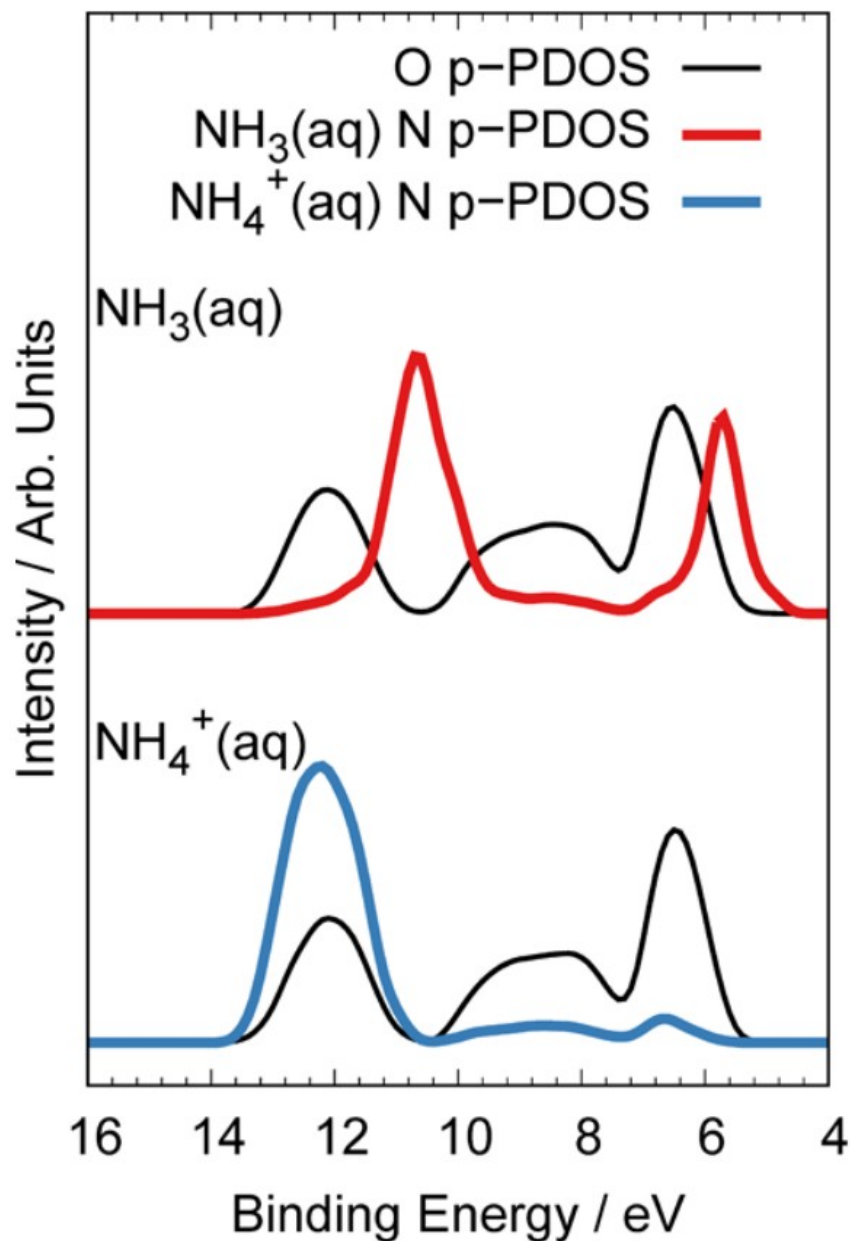


# RIXS spectroscopy of $\text{NH}_3(\text{aq})$



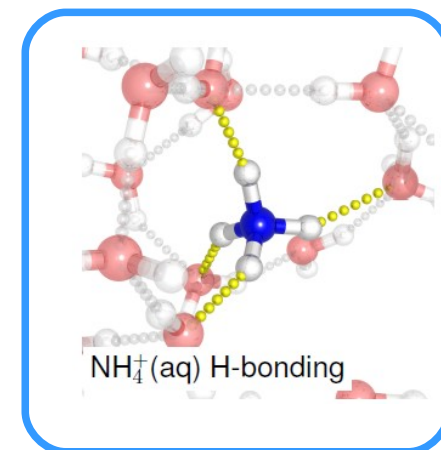
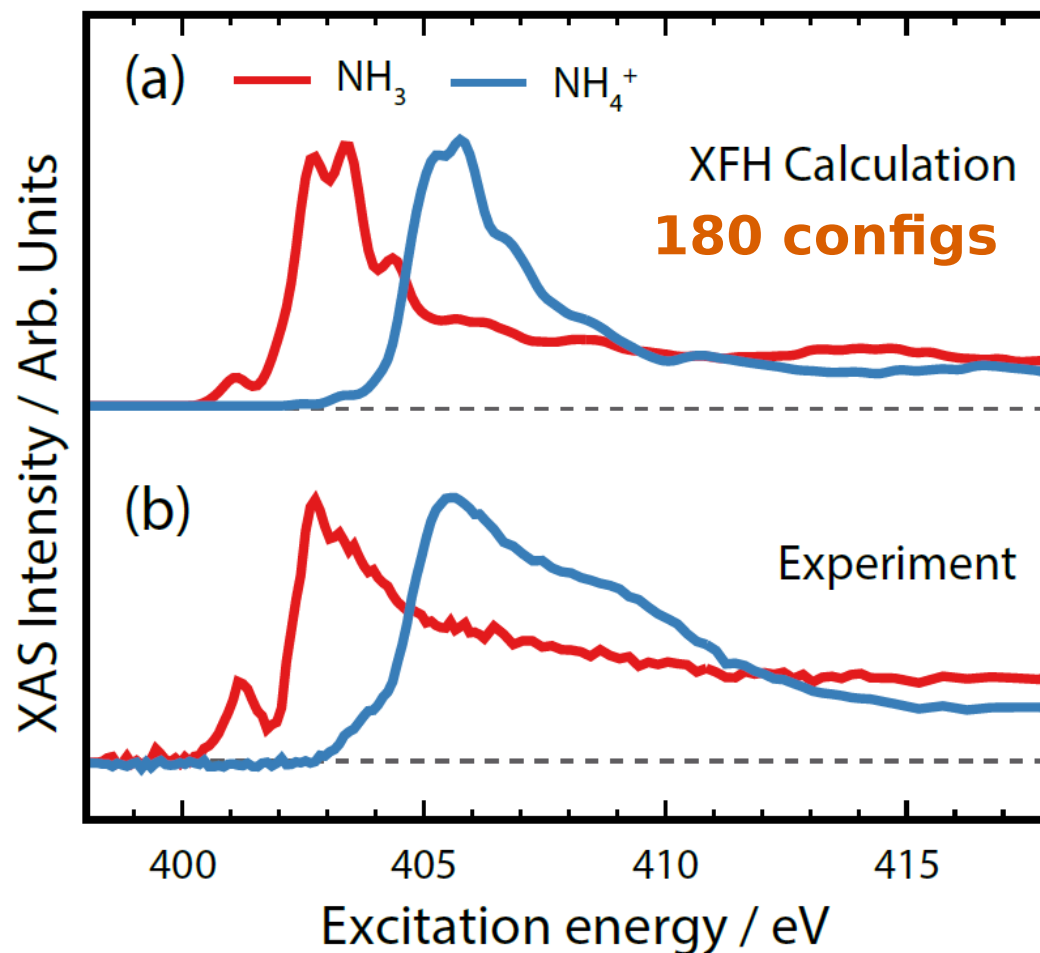
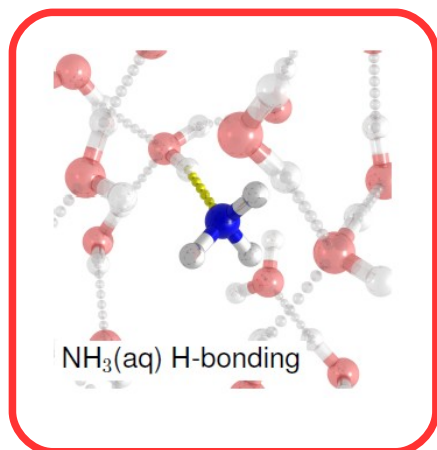
# The effect of pH

Aqueous ammonia: Energy mismatch



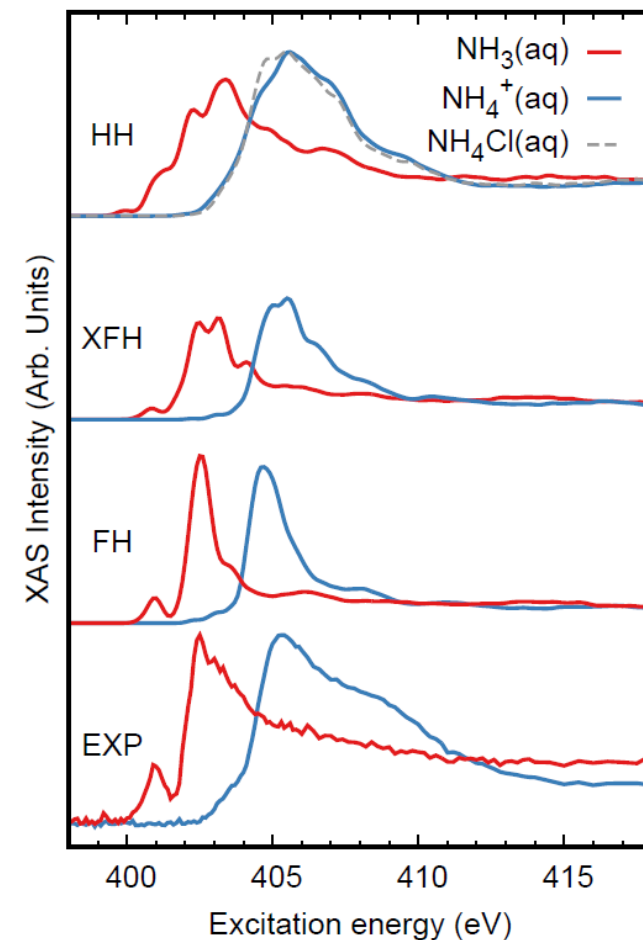
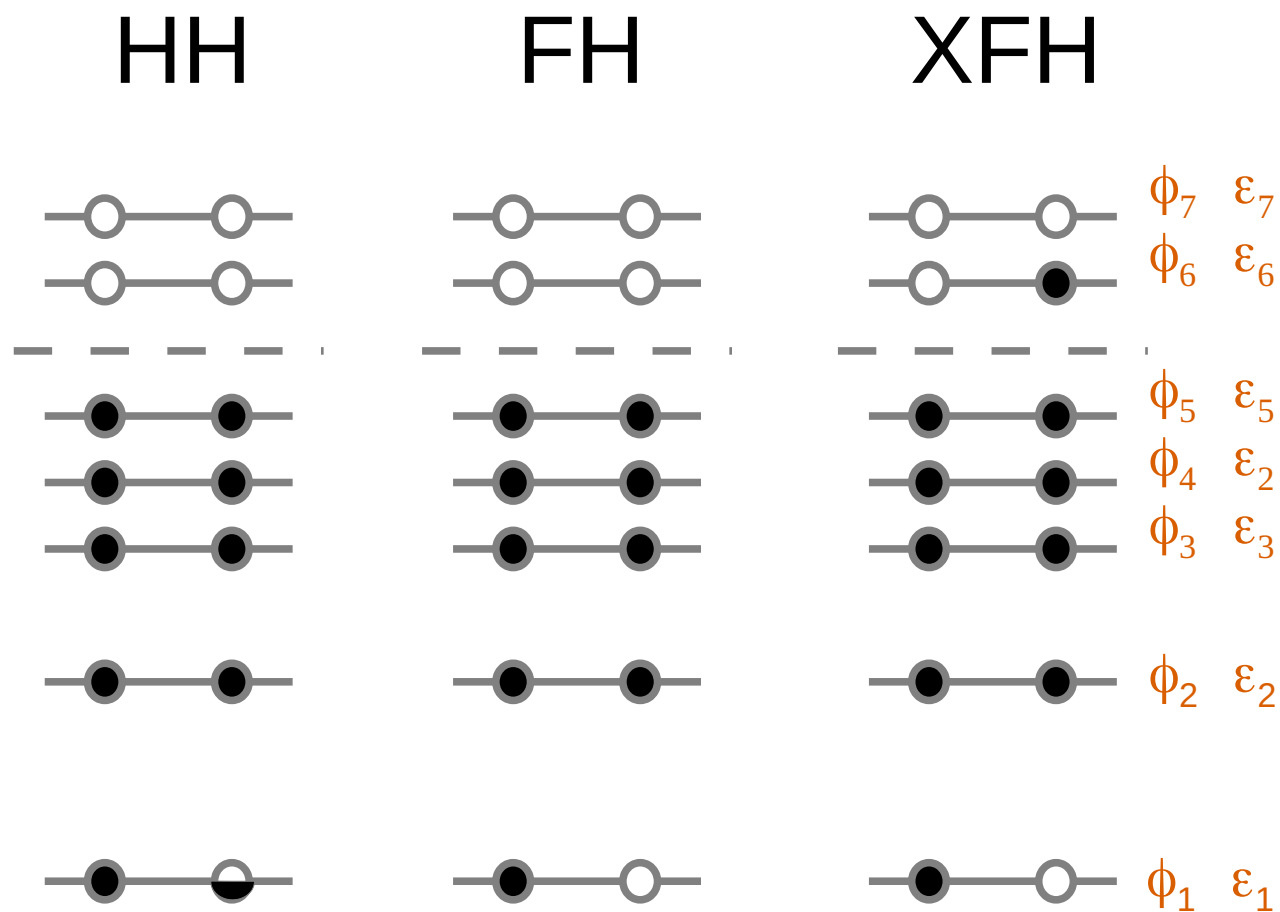
Hydration structure of  $\text{NH}_3(\text{aq})$  and  $\text{NH}_4^+(\text{aq})$ pH dependence in  
N K-edge X-ray absorption

M. Ekimova et al. DOI: [10.1021/jacs.7b07207](https://doi.org/10.1021/jacs.7b07207)  
*J. Am. Chem. Soc.* 2017, 139, 12773–12783



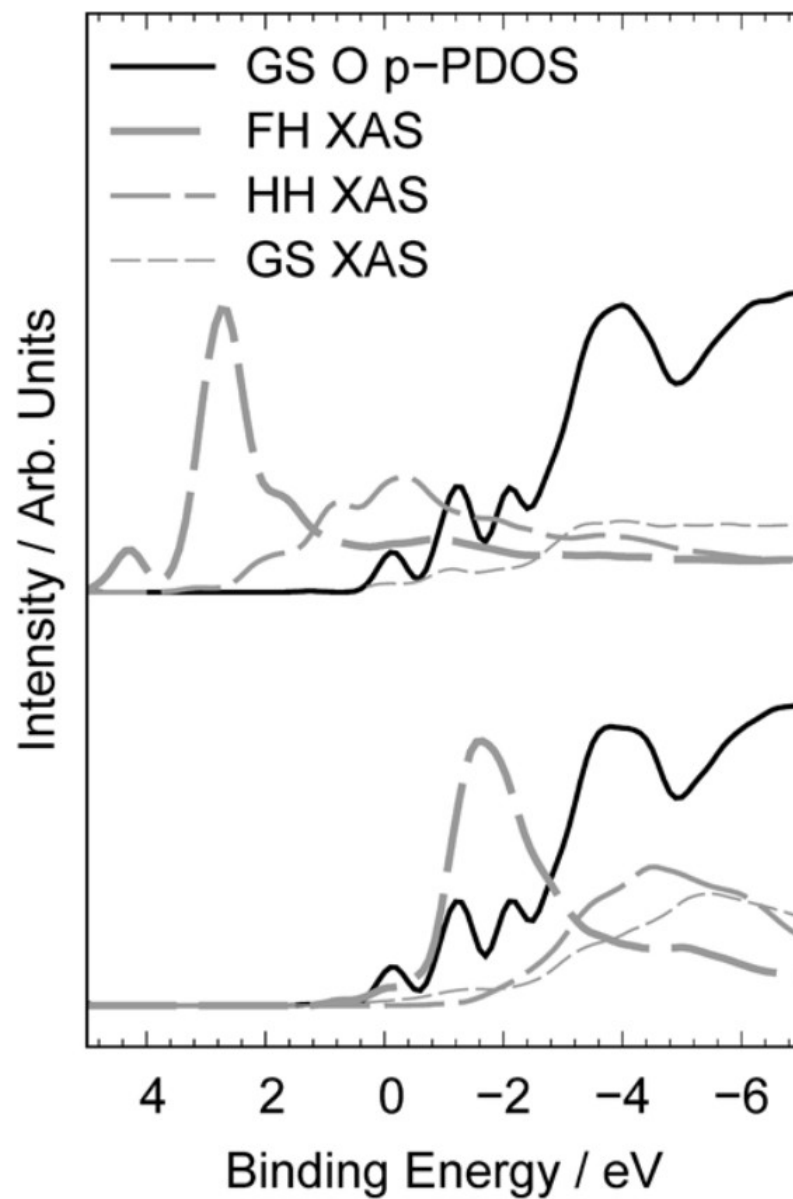


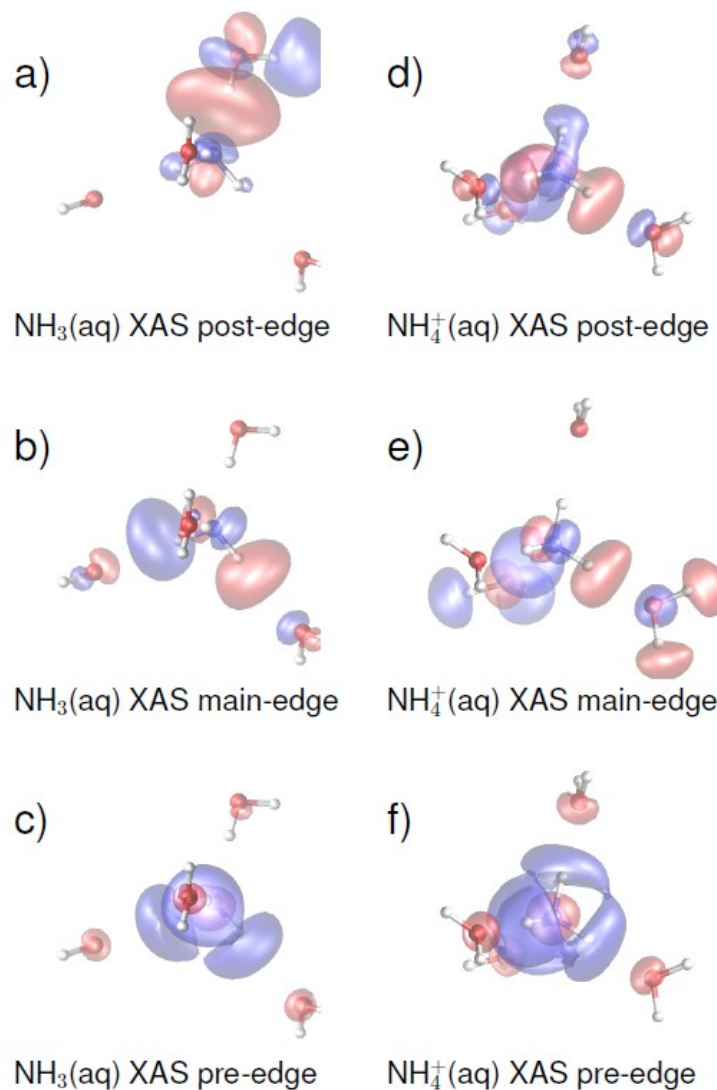
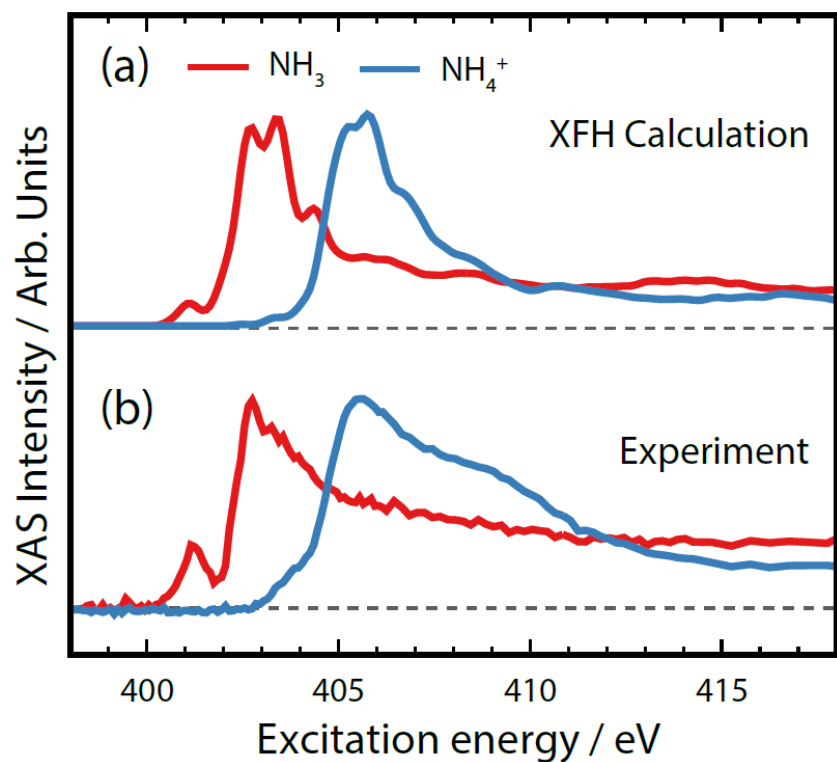
# Transition potential approximations of N K-edge XAS



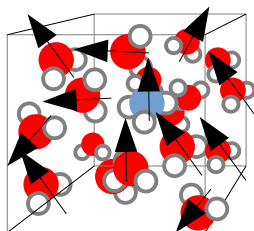
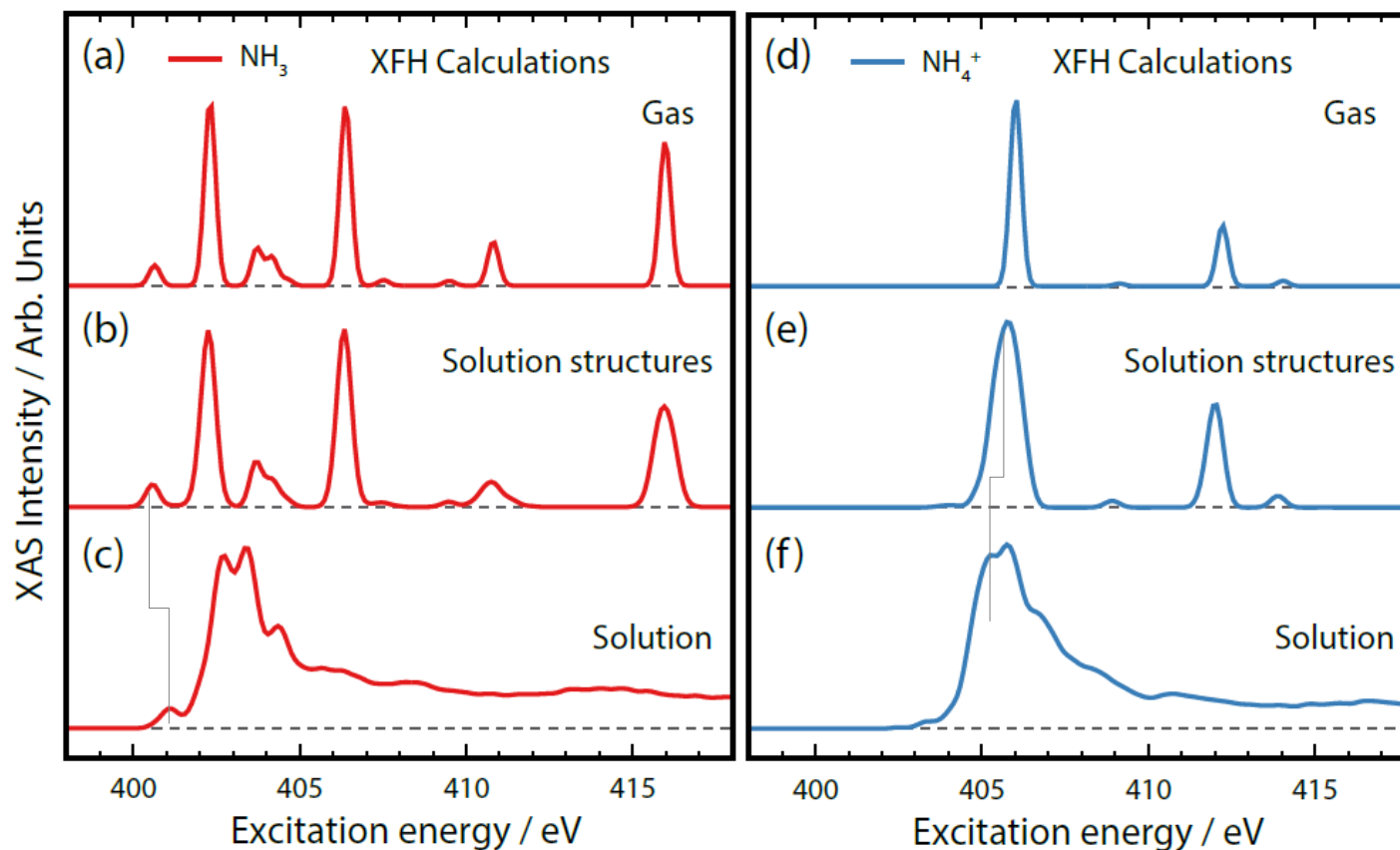
In our case,  
XFH and FH are superior to HH

## Electronic relaxation in the presence of the core-hole



N K-edge XAS of  $\text{NH}_3(\text{aq})$  and  $\text{NH}_4^+(\text{aq})$ 

# N K-edge XAS of $\text{NH}_3(\text{aq})$ and $\text{NH}_4^+(\text{aq})$



## $\text{NH}_3(\text{aq})$ :

Whole XAS blue-shifted by accepting H-bonding

## $\text{NH}_4^+(\text{aq})$ :

Pre-edge intensity due to distortions

Main-edge slightly red-shifted by donating H-bonding

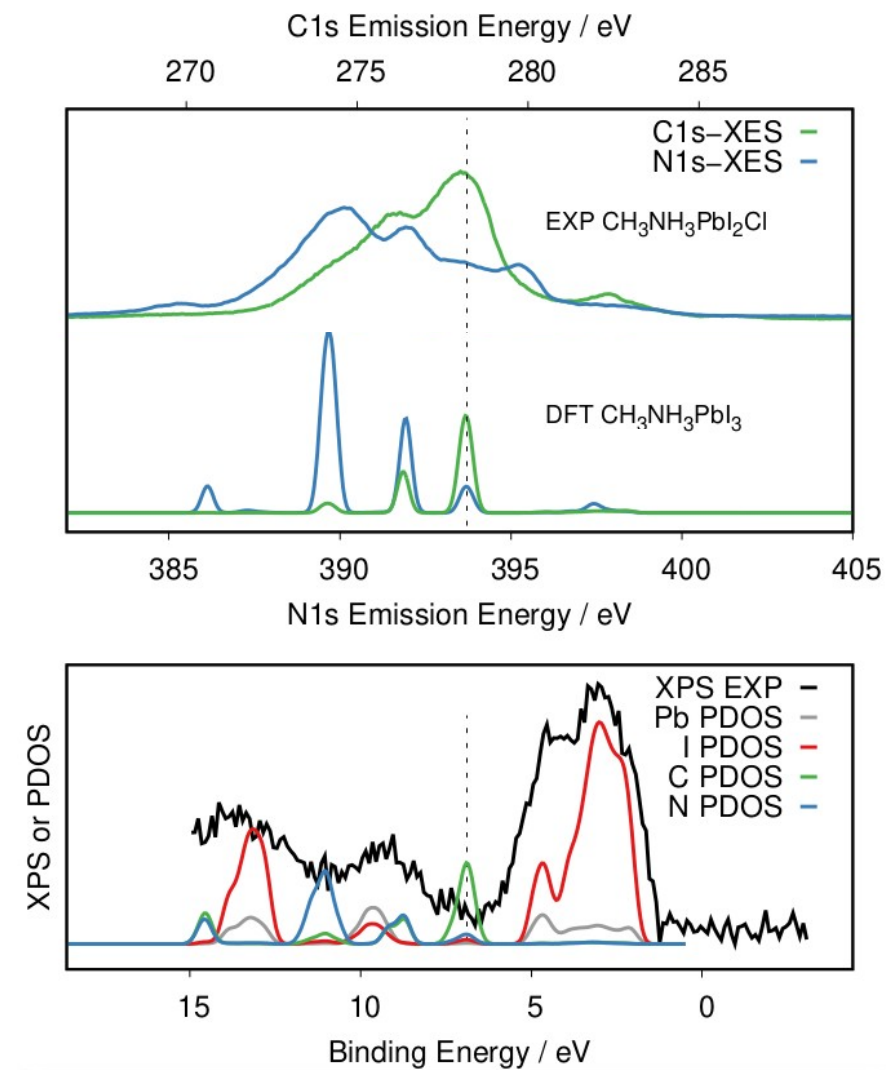
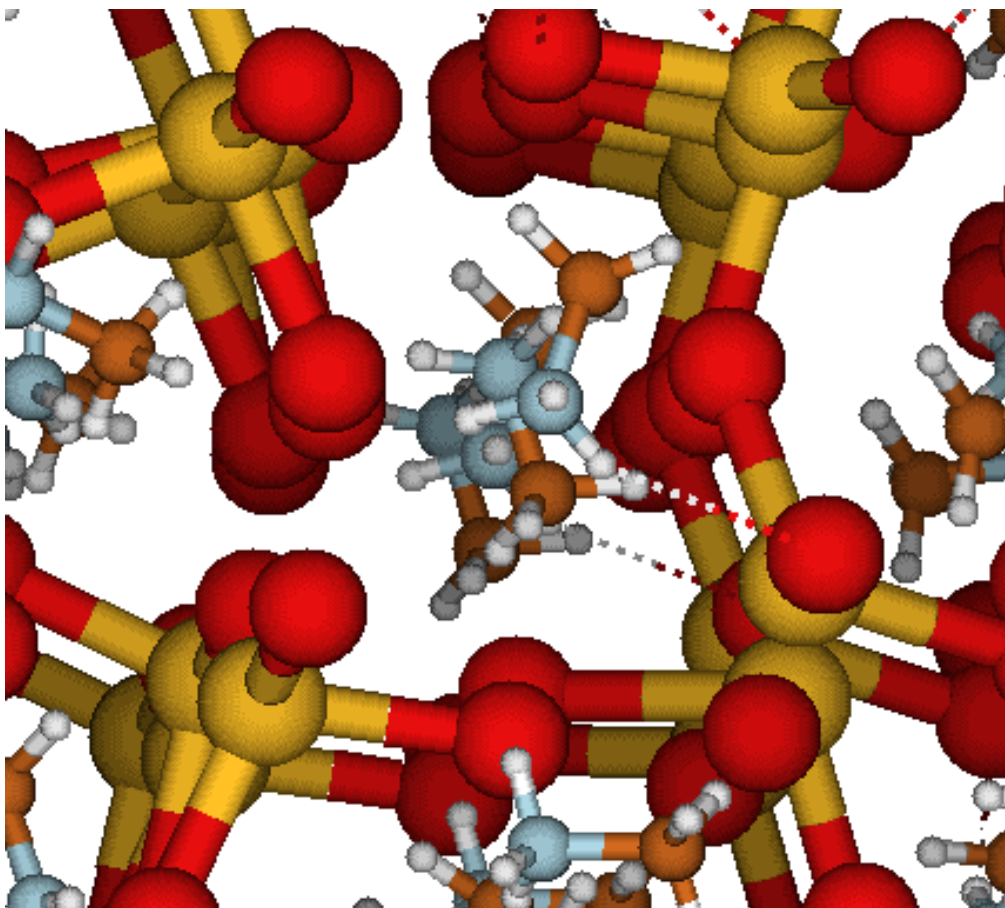
Post-edge not well reproduced



# Perovskite solar cells: $\text{PbI}_3\text{CH}_3\text{NH}_3$

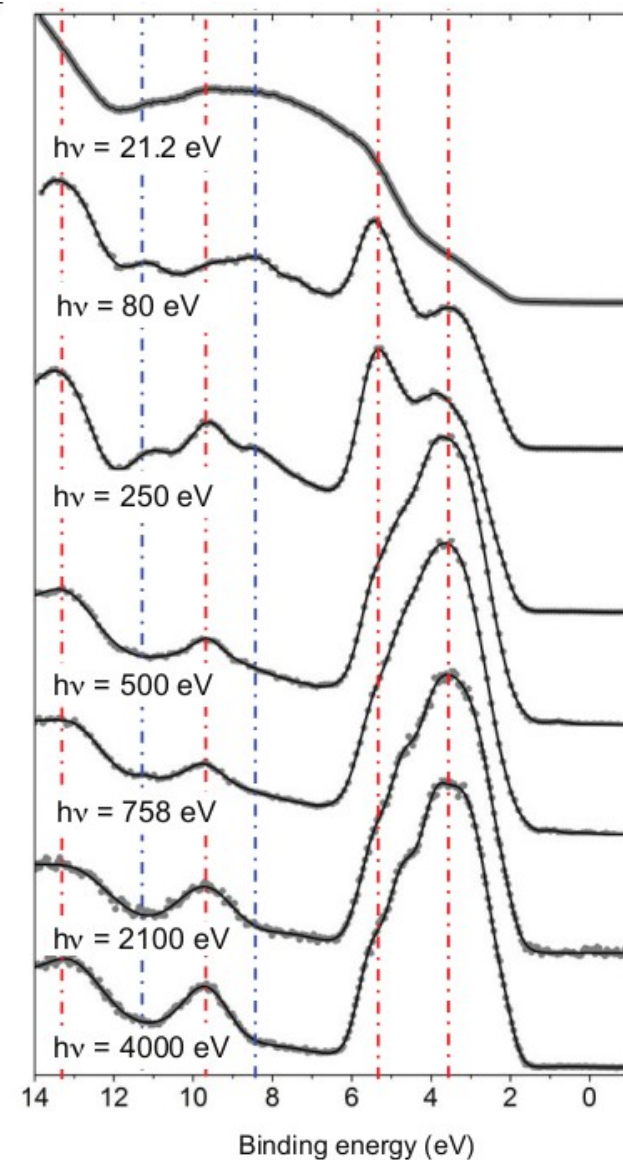
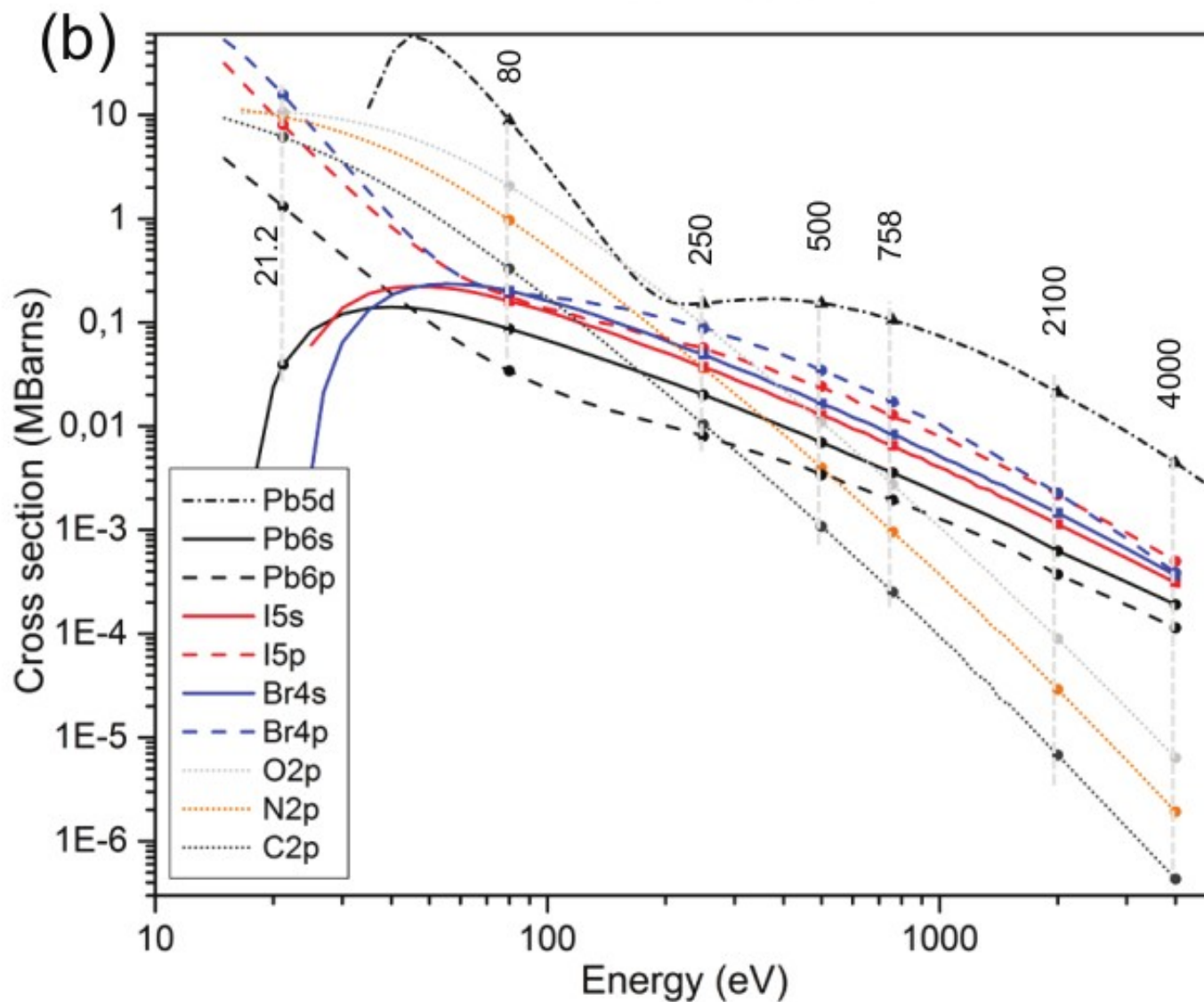
## XPS and XES

R. Wilks, M. Bär ....A. Erbing, M. Odelius



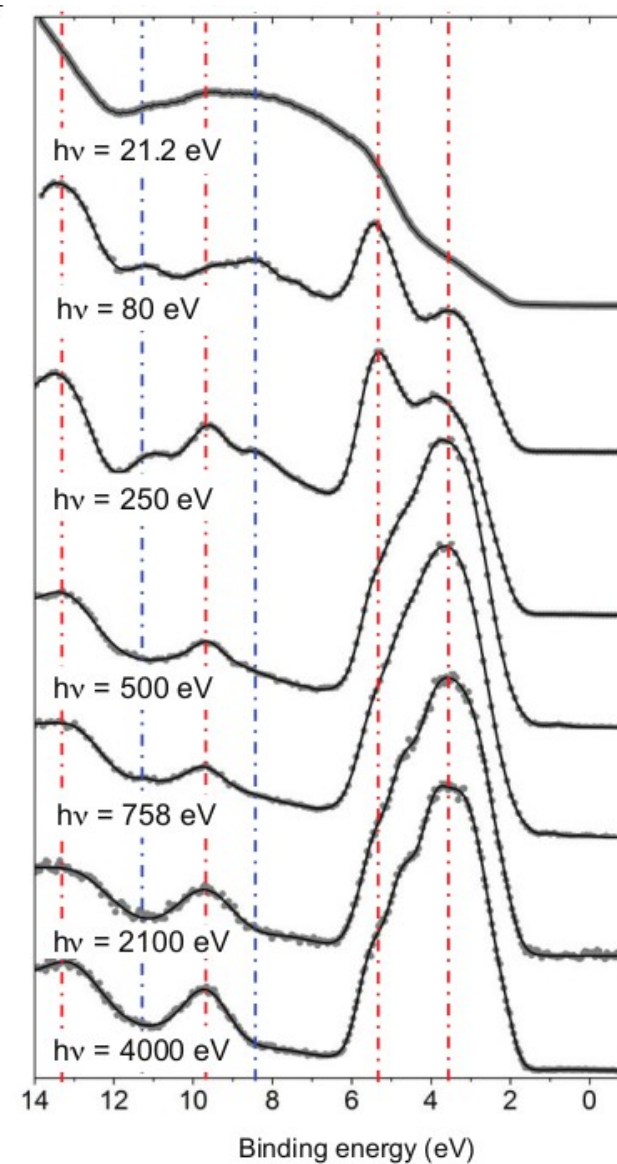
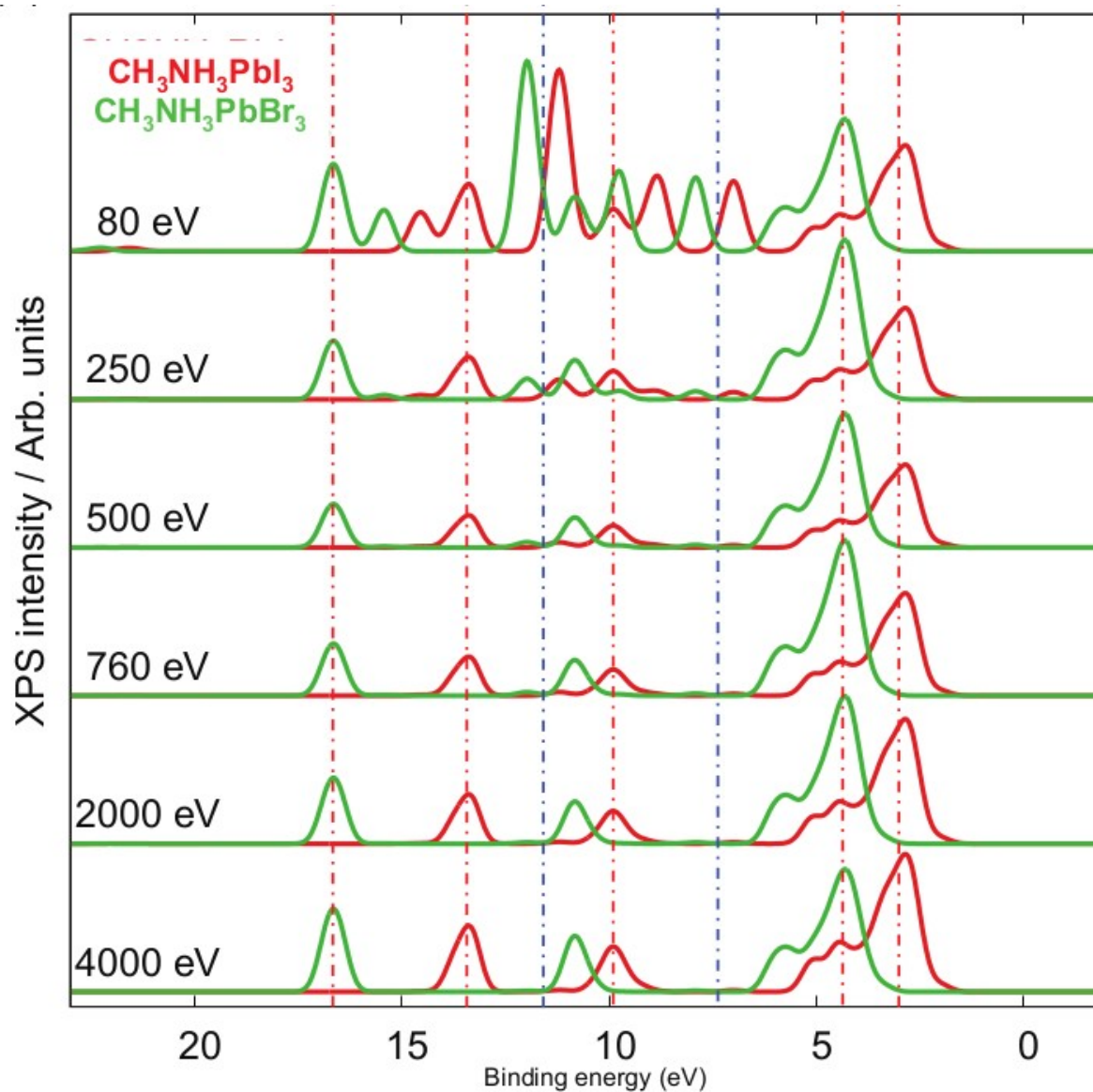
# Perovskite solar cells: $\text{PbI}_3\text{CH}_3\text{NH}_3$

## Photo-energy dependence in XPS

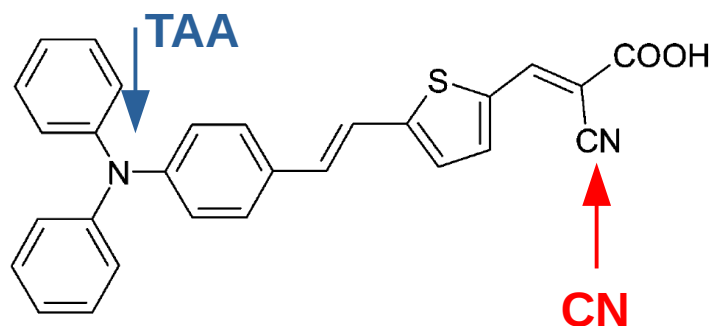


# Perovskite solar cells: $\text{PbI}_2\text{CH}_3\text{NH}_3$

## Photo-energy dependence in XPS

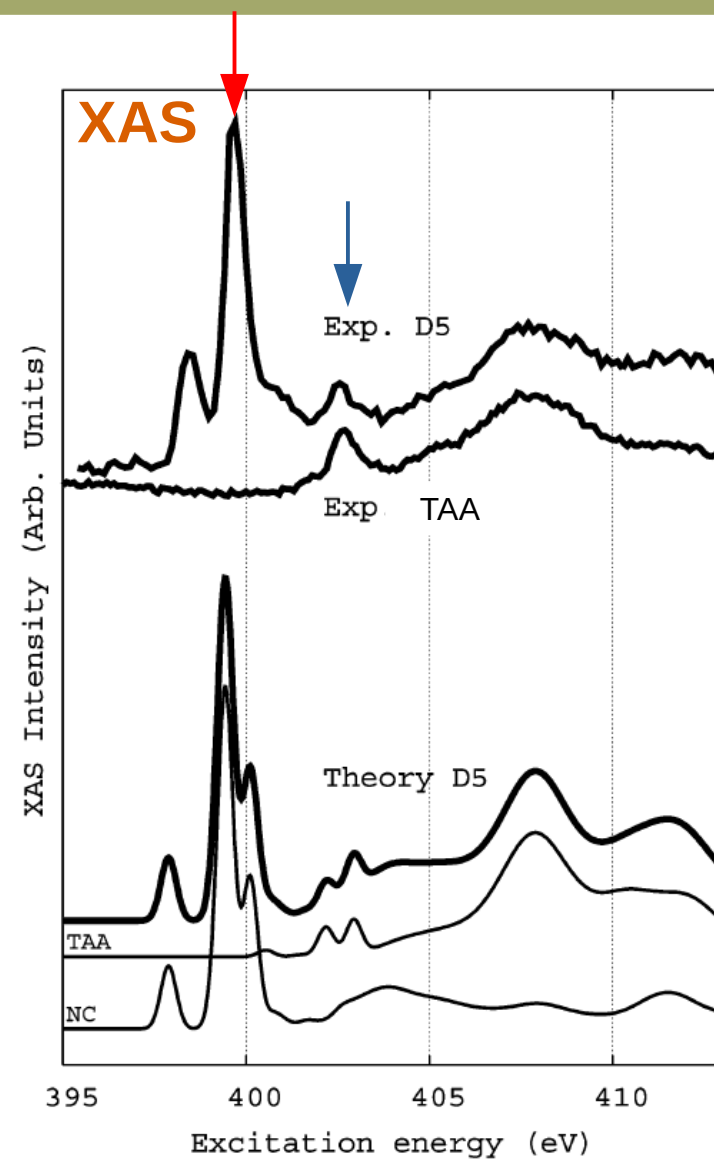
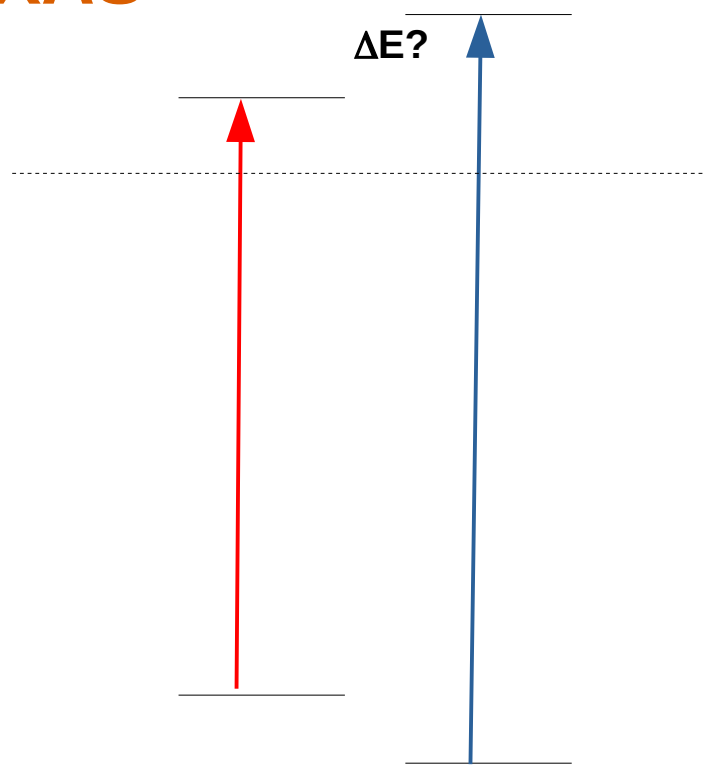


## Orbital energies derived from XAS and XPS of an organic dye



Molecular structure of D5.

XAS

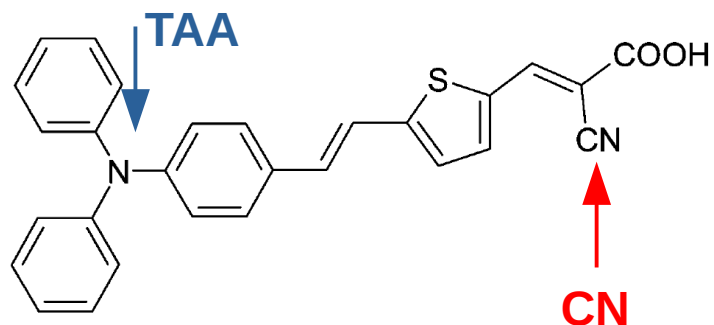


E. Johansson et al

*J. Phys. Chem. C* 2007, 111, 8580–8586

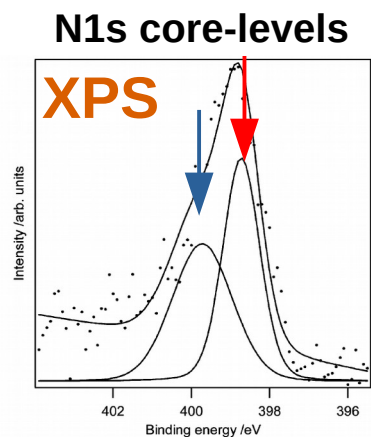
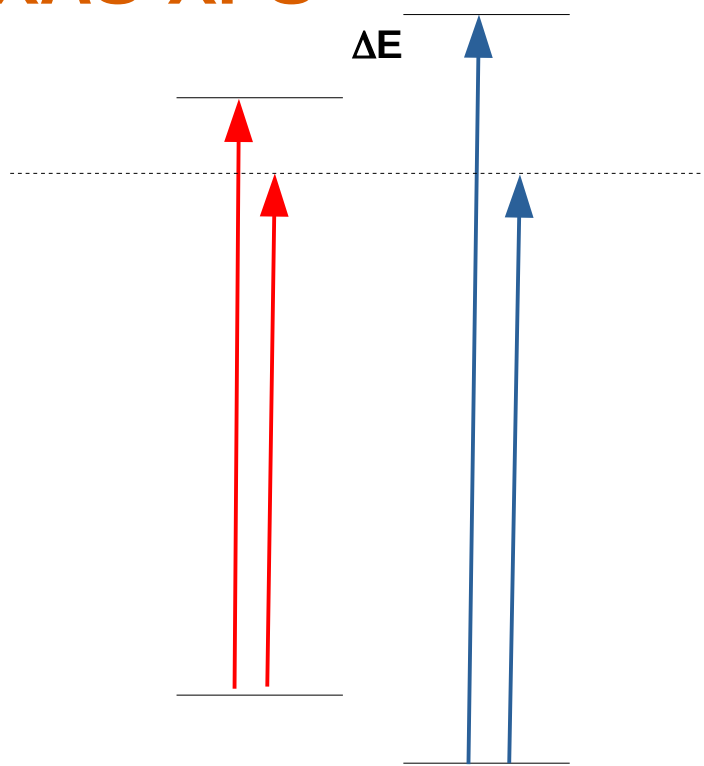


## Orbital energies derived from XAS and XPS of an organic dye



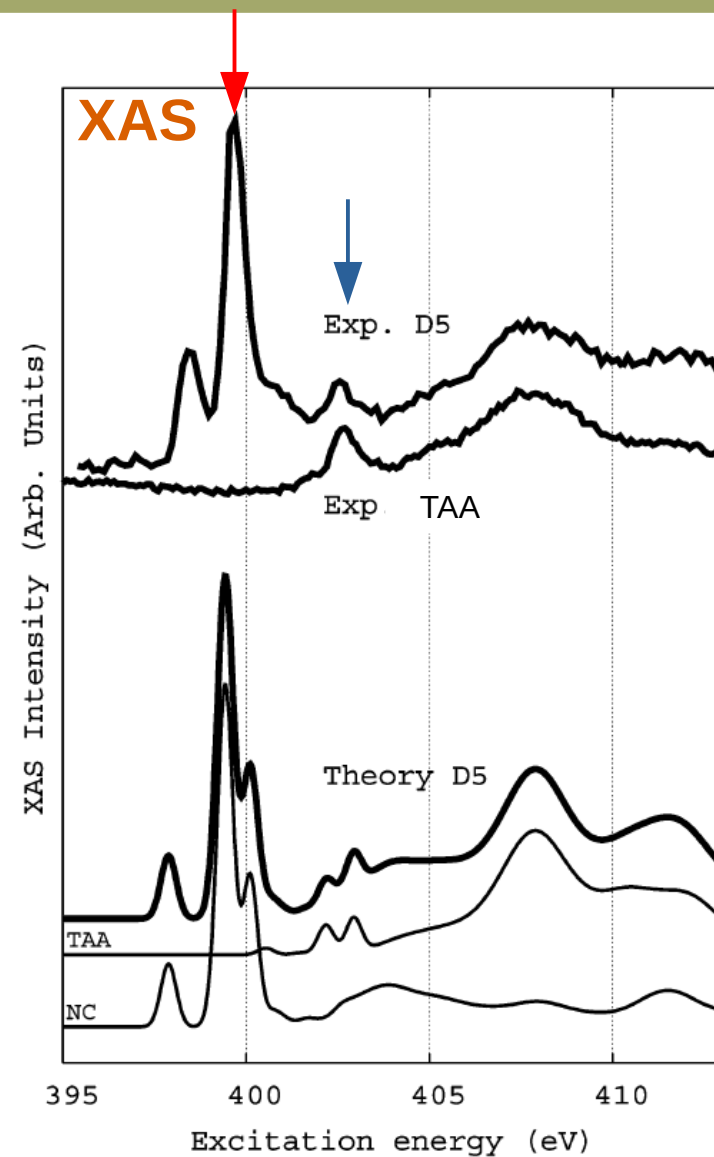
Molecular structure of D5.

## XAS-XPS



Valence XPS  
show that HOMO  
resides on TAA

Lowest UV  
excitation is a  
TAA → CN  
charge transfer



E. Johansson et al

*J. Phys. Chem. C* **2007**, *111*, 8580–8586

# Outline

## Spectrum simulations – Part I

### Molecular orbital representation

**XPS** - Chemical environment  
- Chemical bonding

**XES** - Local element-specific projection

**XAS** - Local element-specific projection  
- Relaxation in presence of core-hole  
- Alignment of energy scales