


# CEOs and the economics of superstars



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**Xavier Gabaix, Harvard**

# Motivation

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- This talk is about the economics of superstars – inequality in income at the very top
- I'll focus first on CEOs (Chief Executive Officers = head of companies)
- Then I'll come back to more general superstars
- And the rest of the economy
- And policy
  
- Thanks to my coauthors: Alex Edmans, Dirk Jenter, Augustin Landier, Yuliy Sannikov, Julien Sauvagnat, Tomasz Sadzik

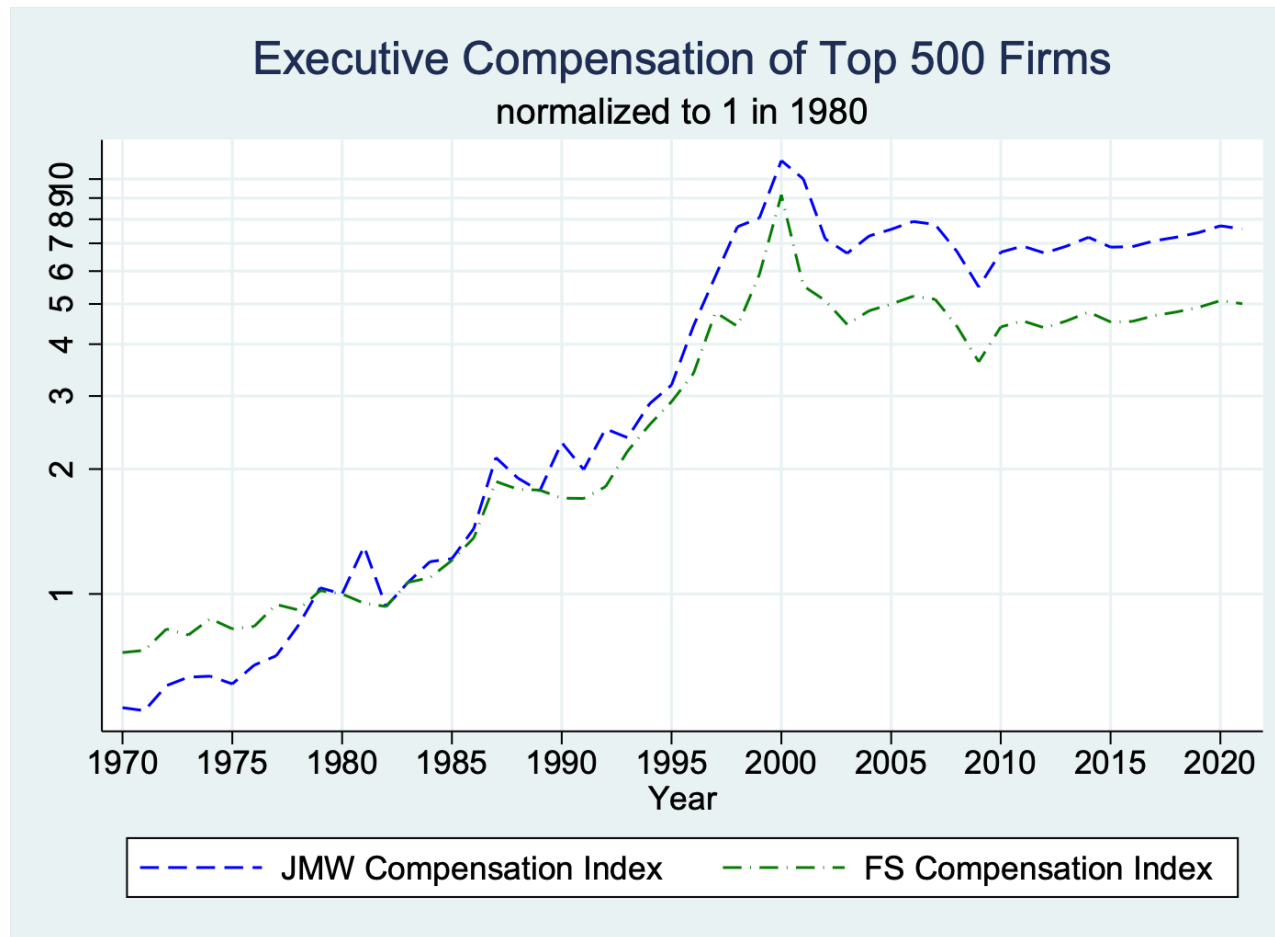
# Why care about CEOs?

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- Large popular and academic focus on the increase of CEO pay in the US since the 80s.
- Lots of good data (from forced disclosure) on CEO pay -> We can do precise work
- I'll start from G. Landier "Why has CEO pay increased so much?" (QJE '08)
- Changes in firm size appear to explain much of the variations in CEO pay, across time (since 1970s at least), industries, countries

# Short Literature Review:

- **Fact 1:** CEO pay has been multiplied by **5 to 7** between 1980 and 2003, with smallish rise afterwards



Source: Jensen Murphy Wruck (2003); Frydman Saks (2010), G. Landier Sauvagnat (2014)

# Short Literature Review:

## Reminder of 2 facts and 3 theories...

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- **Fact 2:** US top CEOs are paid more than their foreign counterparts. (Kaplan (1994), Abowd and D.Kaplan (1998), Fernandes et al. (2013))



# Short Literature Review:

## Reminder of 2 facts and 3 theories...

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### □ **Theory 1: Higher Incentives → Rents**

- Murphy (1985), Jensen-Murphy (1990):  
importance of market-based incentives
- Holmstrom –Kaplan (2001,2003):  
discovery of high-powered incentives in the 80s?

**Need strong *limited liability & risk-aversion* frictions to explain such higher *rents*.**

(calibration: e.g. Gayle & Miller 2009, 2015)

# Short Literature Review:

## Reminder of 2 facts and 3 theories...

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### □ **Theory 2: “Skimming View”**

- Bertrand Mullainathan (2001), Kuhnen Zwiebel (2009)
- Bebchuk Fried (2004)
  - Increased entrenchment & “camouflage” techniques
- Hall Murphy (2003), Jensen Murphy Wruck (2004)
  - Boards underestimate the cost of stock-options
- Difficulties with that view:
  - Governance seems to have improved, not worsened
  - Private equity firms pay their CEOs a lot, even more than publicly traded firms (Kaplan Rauh 2013, Cronqvist Fahlenbrach 2013)

# Short Literature Review:

Reminder of 2 facts and 3 theories...

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## □ **Theory 3: Changes in CEO job/labor market**

- Murphy and Zabojnik (2004), Frydman (2005)
  - Higher importance of general (vs. specific) skills
    - higher CEO outside options, more external hires
- Garicano and Rossi-Hansberg (2006)
  - Technological change and hierarchies in equilibrium
- See also Bertrand and Schoar (2003), Bloom et al. (2006), Daines, Nair, Kornhauser (2005), Malmendier and Tate (2005), Geerolf (2018)



# Our Approach: the “Size of Stakes” View

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- Focus on one important source of variation:
  - ***firm size***
  
- Assortative matching of firms and managers
  - Lucas (1978), Sattinger (1979), Rosen (1981,82), Himmelberg and Hubbard (2000), Tervio (2008)
  
- Frictionless talent market
  
- CEO pay = price of talent
  - Depends on:
    - Asset distribution
    - Production function
    - Talent distribution (unobservable!)
  
- General results using Extreme Value Theory

# CEO Pay in Equilibrium

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- $N$  firms to match with  $N$  managers
  - Firms have size  $S(m)$  (*descending order*)
  - Managers talent  $T(n)$ , paid  $w(n)$  in equilibrium.
- Firm's Program: Hiring the CEO increases earnings by:

$$\max_n C \times \underbrace{T(n) \times S^\gamma}_{\text{CEO impact}} - w(n)$$

*Price of talent #n*

- Relevant size measure?
  - **Permanent CEO impact** → **S=market value (D+E)**
  - Temporary CEO impact → S=earnings
- Benchmark case: constant returns of talent
  - $\gamma=1$ , empirically validated

# Equilibrium:

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An equilibrium consists of:

- (i) a compensation function  $W(T)$ , which specifies the wage of a CEO of talent  $T$
- (ii) an assignment function  $M(m)$ , which specifies the index  $n=M(m)$  of the CEO heading firm  $m$  in equilibrium, such that
- (iii) each firm chooses its CEO optimally:

$$M(m) \in \arg \max_n C \times S(m)^\gamma \times T(n) - W(T(n))$$

- (iv) the CEO market clears, i.e. each firm gets a CEO.

# Equilibrium:

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□ First order condition:  $C \times S(m)^\gamma \times T'(n) = w'(n)$

□ **Assortative matching:**

- Firm **#n** is matched with manager **#n**

$$\Rightarrow w(n) = w(N) - \int_n^N C \times S(m)^\gamma \times T'(m) dm$$

<0

□ Equilibrium wages depend on

- Productivity
- Scarcity of talent

□ How do we go further?

# Distributions

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## □ Firms: observable

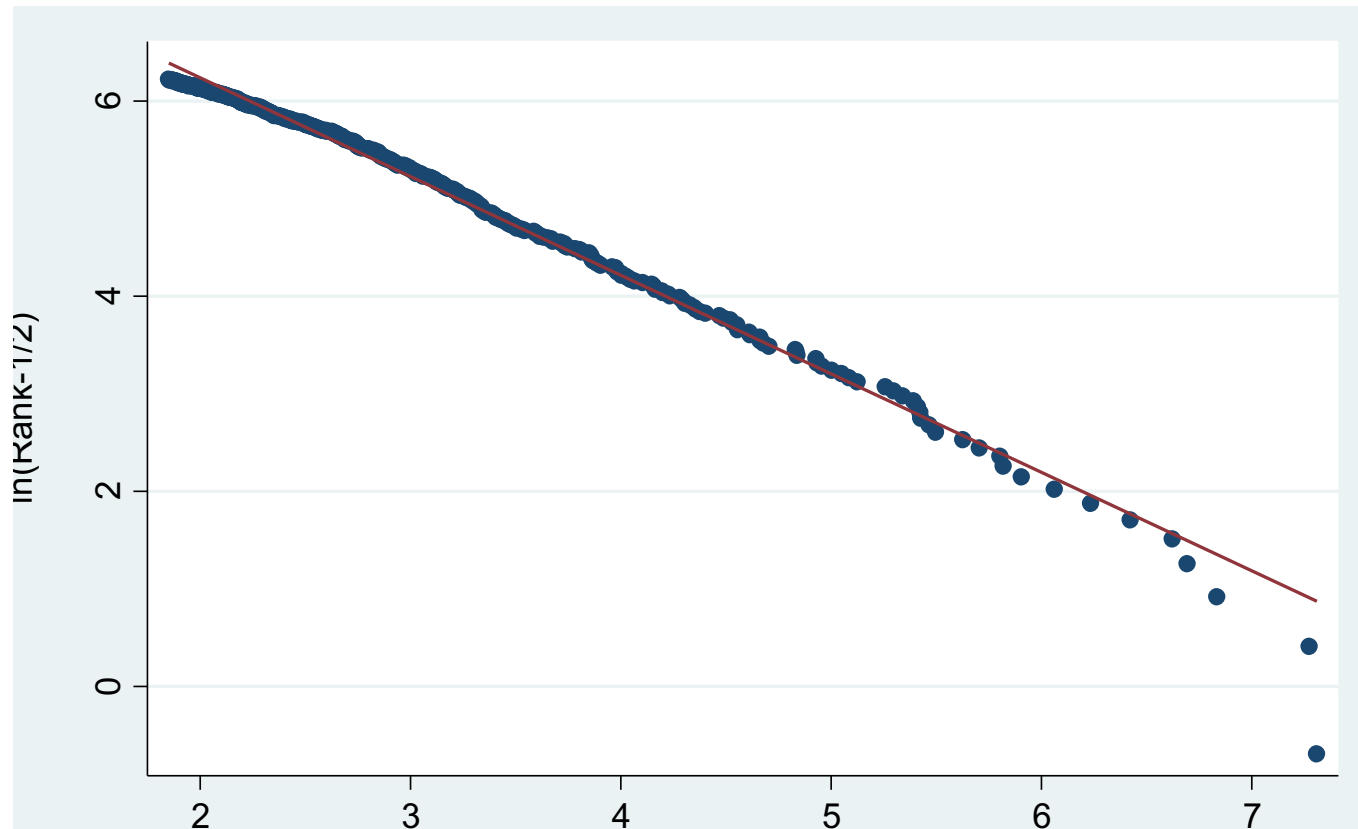
$$S(n) = \frac{A}{n^\alpha}$$

- Useful for calibration: Zipf's law

$$(\alpha \approx 1)$$

- Simon (1955), Gabaix (1999, 2009 and ref. therein), Axtell (2001), Luttmer (2005, 2018), Axtell and Guerrero (2022)...

# Zipf's law for size (market value) of firms



- Largest 500 firms in the US in 2004
- $\ln(\text{Rank}-1/2) = a - 1.01 \ln \text{Size}$ ,  $R^2=0.99$
- (Rank-1/2: Gabaix Ibragimov 2011)

# Distributions

$$w(n) = w(N) - \int_n^N C \times S(m)^\gamma \times T'(m) dm$$

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**Talent: unobservable** → use *Extreme Value Theory*

$$T'(n) = -Bn^{\beta-1}$$

- Valid approximation for all “regular” distributions
  - ▣ Gaussian, log-normal, Weibull, log-gamma, etc.
- Exact for uniform, exponential, Pareto

# Main Proposition

$$S(m) = Am^{-\alpha}, -T'(m) = Bm^{\beta-1}$$

$$w(n) = w(N) - \int_n^N C \times S(m)^\gamma \times T'(m) dm \rightarrow w(n) = \frac{A^\gamma BC}{\alpha\gamma - \beta} \times \frac{1}{n^{\alpha\gamma - \beta}}$$

□ Using def. of A and B, get:

$$w(n) = D \times S_{n^*}^{\beta/\alpha} \times S_n^{(\gamma - \beta/\alpha)}$$

$$w(n) = D \times S^{\uparrow 1/3} \times S_*^{\uparrow 2/3}$$

Own Firm Size

Reference Size

Can be country specific

$$D = \frac{-n_* T'(n_*)}{\alpha\gamma - \beta} \times C$$



# Main Predictions $w(n) = D \times S_{n^*}^{\beta/\alpha} \times S_n^{(\gamma-\beta/\alpha)}$

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- Cross-sectional: (change  $n$ )

$$w(n) = (cste) \times S_n^{(\gamma-\beta/\alpha)}$$

- Cross-time: (change  $A$  in  $S(n) = A/n^\alpha$ , keep  $n$  constant)

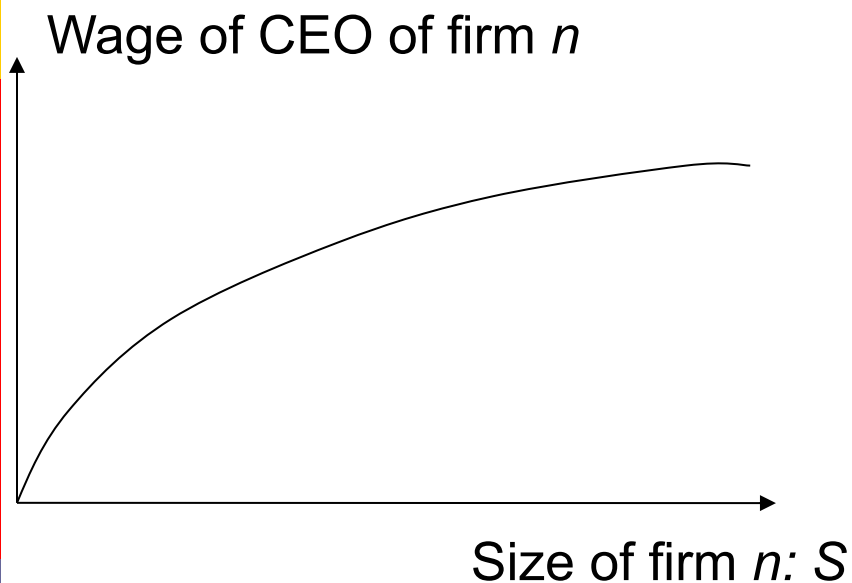
$$w(n^*) = (cste) \times S_{n^*}^\gamma$$

- Cross-country: (keep  $S(n)$  & *Pop. Size* constant)

$$w(S) = (cste) \times S_{n^*}^{\beta/\alpha}$$

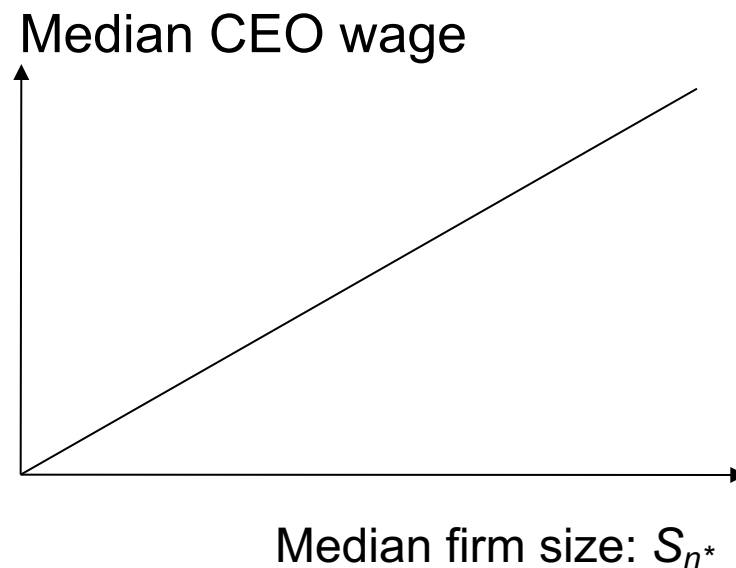
# Main Predictions

$$w(n) = D \times S_{n^*}^{2/3} \times S_n^{1/3}$$



**Cross-section:** Wage is a **concave** function of size:

$$w_n = k S_n^{1/3}$$



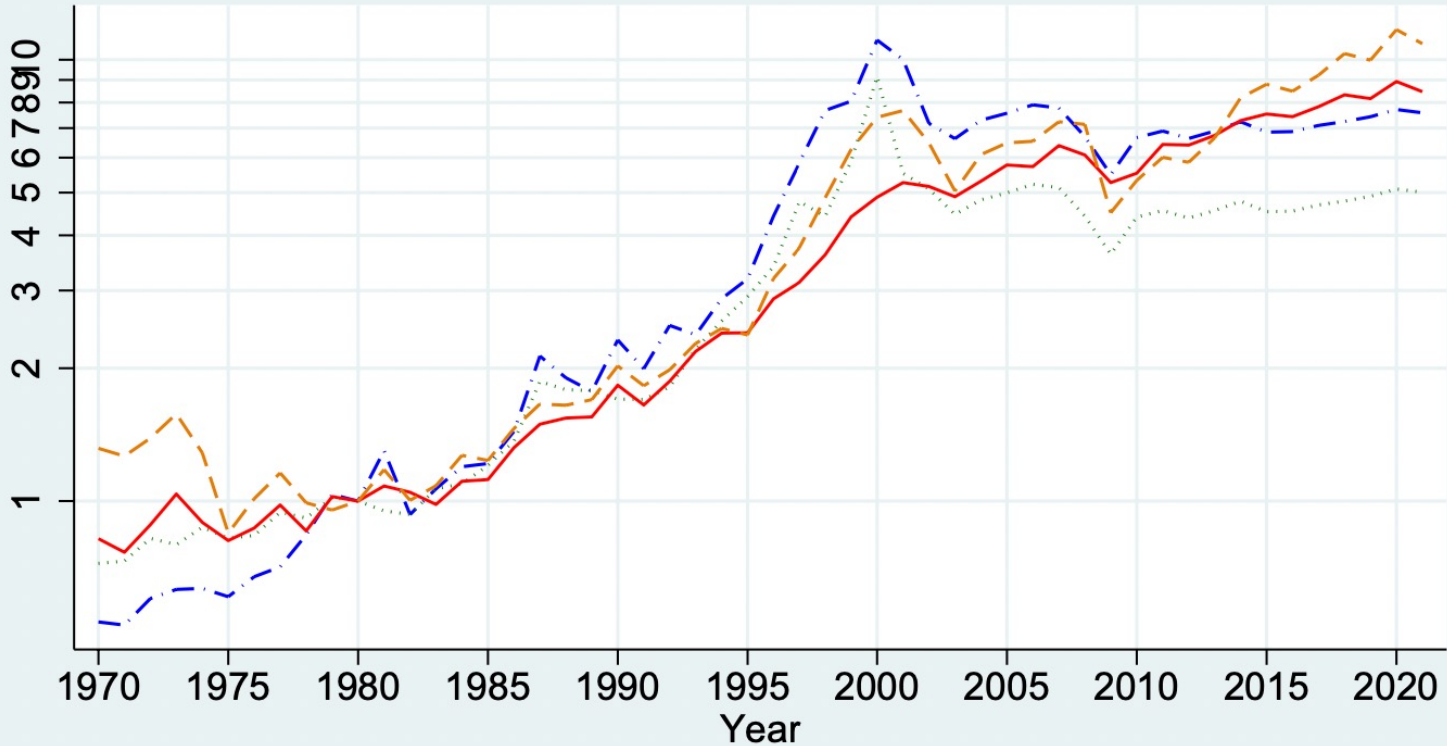
**Time series:** Aggregate wage is a **linear** function of aggregate size:

$$w_{n^*} = k' S_{n^*}$$

The relationship between size and pay is very different in the cross section and the time-series

# Update (G, Landier, Sauvagnat 2014)

Executive Compensation and Size of Top 500 Firms  
normalized to 1 in 1980



--- JMW Compensation Index      ..... FS Compensation Index  
—— TOP 500 Firm Value      - - - - TOP 500 Equity Value

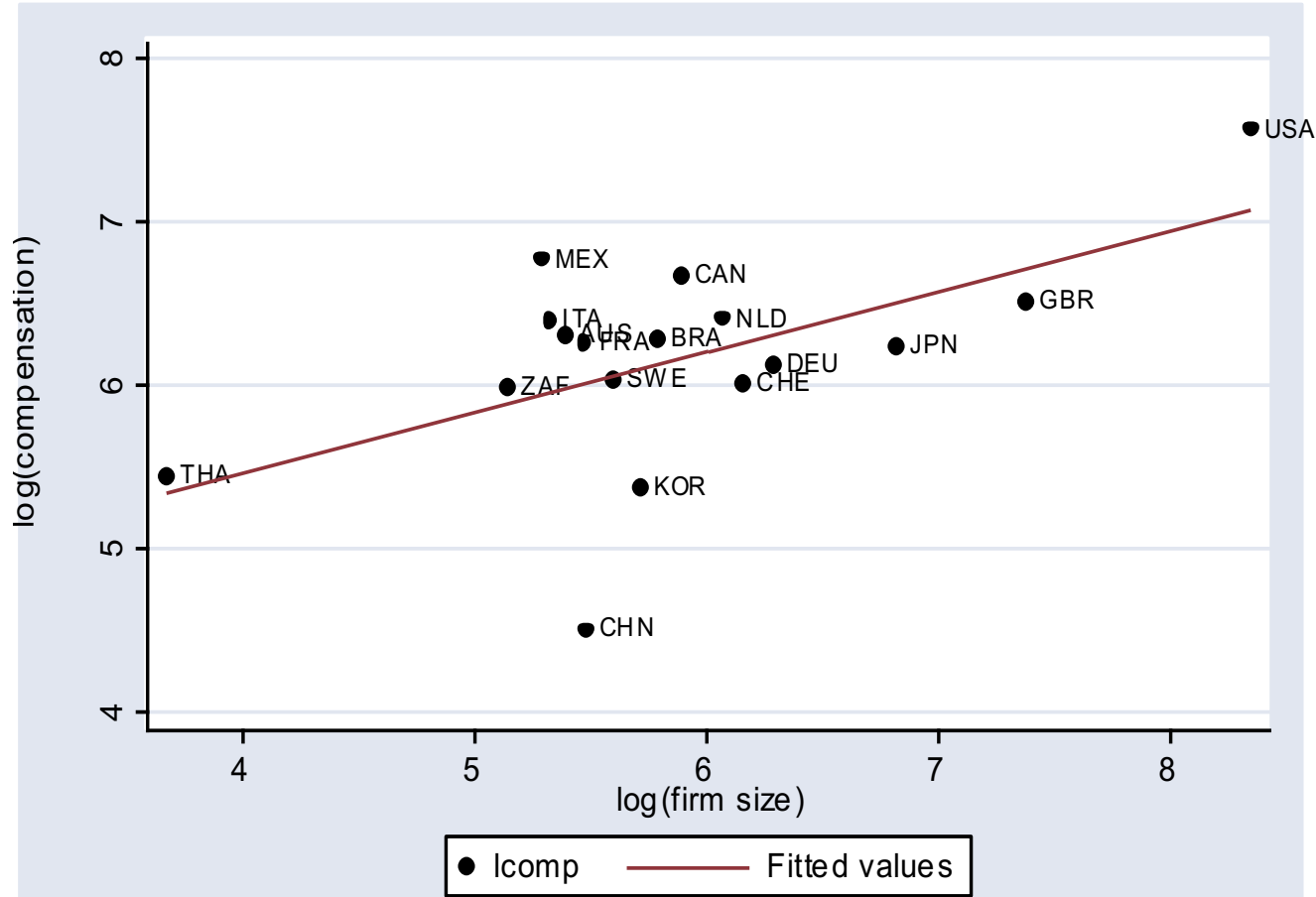
Thanks to J. Sauvagnat for the update

Panel Evidence: USA, 1992-2004

$$w_n = D \times S_n^{(\gamma - \beta/\alpha)} \times S_{n^*}^{\beta/\alpha}$$

|                             | ln(total compensation)    |                           |                           |                          |
|-----------------------------|---------------------------|---------------------------|---------------------------|--------------------------|
|                             | Top 1000                  |                           |                           |                          |
| ln(Market cap)              | .37<br>(18.28)<br>(24.20) | .37<br>(18.84)<br>(25.13) | .38<br>(16.59)<br>(29.94) | .26<br>(4.60)<br>(6.14)  |
| ln(Market cap of firm #250) | .72<br>(13.60)<br>(10.70) | .66<br>(12.22)<br>(10.06) | .68<br>(11.37)<br>(10.84) | .78<br>(14.97)<br>(9.71) |
| GIM governance index        |                           |                           | 0.019<br>(1.80)<br>(6.82) |                          |
| Industry Fixed Effects      | NO                        | YES                       | YES                       | NO                       |
| Firm Fixed Effects          | NO                        | NO                        | NO                        | YES                      |
| Observations                | 7661                      | 7661                      | 6257                      | 7661                     |
| R-squared                   | 0.22                      | 0.29                      | 0.32                      | 0.60                     |

# Empirical Evidence: cross-country



**Source: Towers-Perrin (2001) for CEO compensation  
Compustat Global (2000) for firm size**

# Empirical Evidence: cross-country

|                       | ln(total compensation) |                 |               |                 |
|-----------------------|------------------------|-----------------|---------------|-----------------|
| ln(median net income) | 0.38<br>(3.7)          | 0.41<br>(4.2)   | 0.36<br>(3.8) | 0.36<br>(3.1)   |
| ln(pop)               |                        | -0.16<br>(1.76) |               |                 |
| ln(gdp/capita)        |                        |                 | 0.12<br>(1.8) |                 |
| “Social Norm”         |                        |                 |               | -0.018<br>(1.5) |
| Observations          | 17                     | 17              | 17            | 17              |
| R-squared             | 0.48                   | 0.57            | 0.58          | 0.52            |

Social Norm= mean agreement to

*“We need large income differences as incentives for individual effort”*

in World Value Survey, 1990. S.e. of Social Norm is 10.

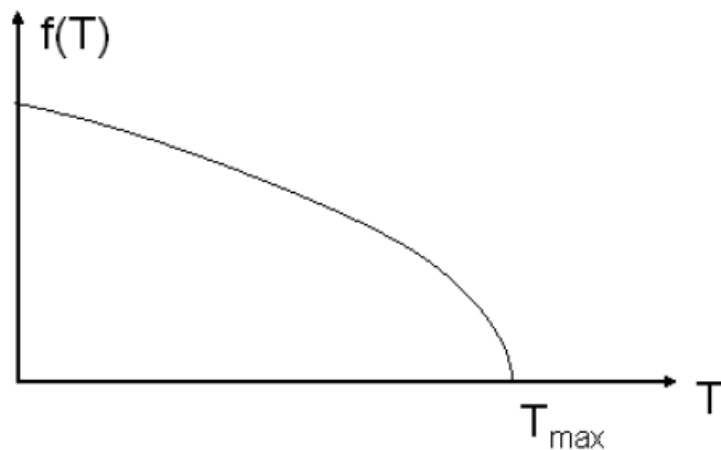
# Calibration, I

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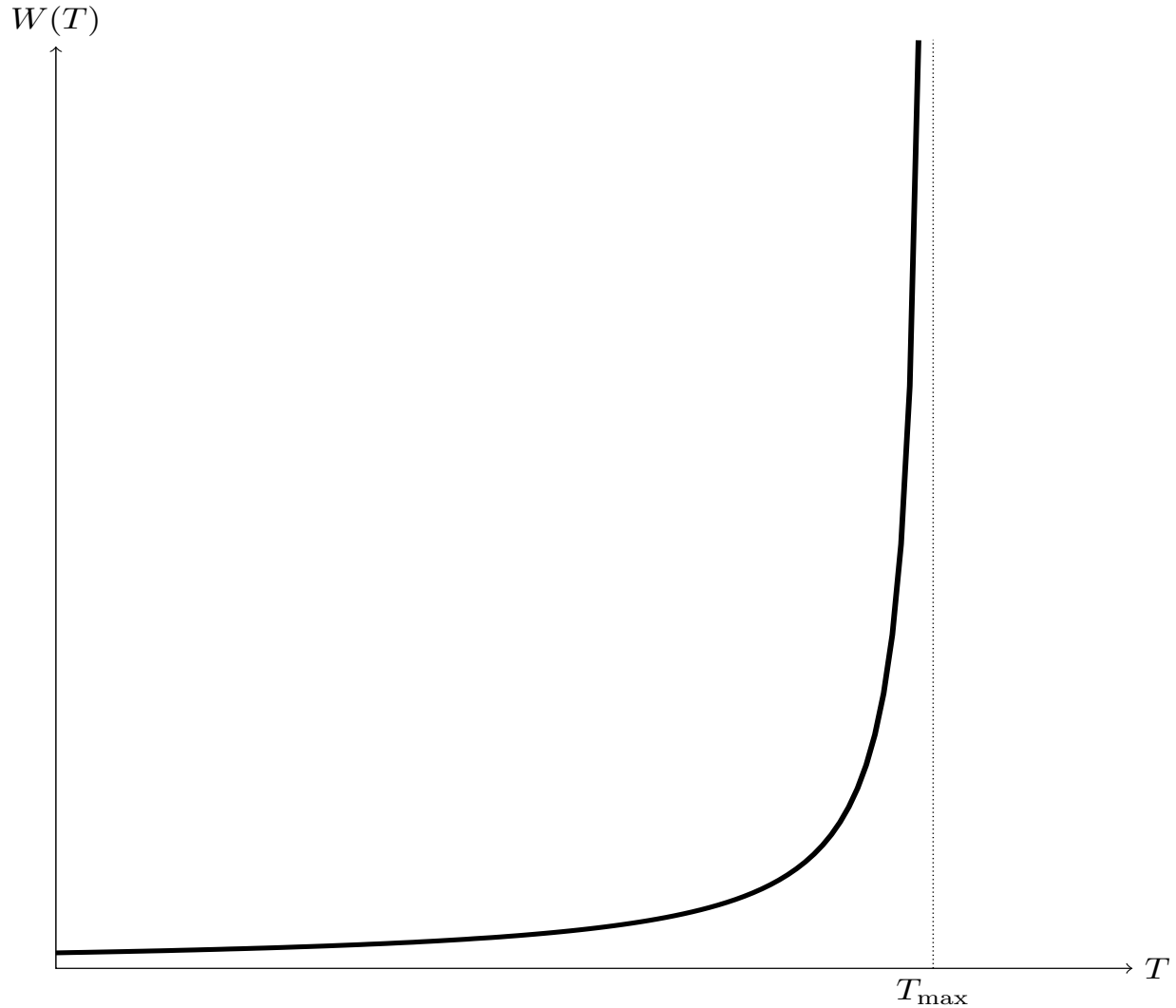
- $\alpha=1$  (Zipf's law)
- $\gamma =1$  from time-series
- Distribution of talent:  $w \sim S^{1/3}$

$$\frac{1}{3} = \gamma - \frac{\beta}{\alpha} \rightarrow \beta=2/3 \rightarrow f(T) = k(T_{\max} - T)^{1/\beta-1} = k(T_{\max} - T)^{1/2}$$

- It would be interesting to compare to: movie stars, lawyers pianists, sport stars...



Wage  $W(T) \sim (T_{max} - T)^{-1/2}$  as a function of talent  $T$



Conclusion for all of us: work hard and accumulate talent, the rewards are very large (unbounded here)



# Calibration, II

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- Take year=2004. Look at median of *top 500* firms and top CEOs. A la Tervio ('08)
  - $n^* = 250$ :  $W(n^*) = \$8.3$  Mil,  $S^* = \$25$  Bil

$$\Rightarrow BC = (\alpha - \beta) \frac{w_* n_*^{-\beta}}{S_*} = 2.6 \times 10^{-6}$$

- Interpretation: #1 CEO, compared to #250 CEO

- increases market value by:

$$C(T(1) - T(250)) = \frac{BC}{\beta} \times (250^\beta - 1) = 0.02\%$$

- Gets paid more by:

$$\frac{w}{w_*} - 1 = \left( \frac{S}{S_*} \right)^{1/3} - 1 \approx 250^{1/3} - 1 \approx 500\%$$

# Calibration, II'

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- This small differential in talent is a robust implication
- Suppose that there's a CEO who can increase value of firm 250 by 1%
- She's worth  $S^* \times 1\% = \$25B \times 1\% = \$250$  million
- As the CEO is paid "only" \$8 million, she must increase the pay by  $<0.1\%$
- So, the differential of  $\sim 0.02\%$  makes sense.

# Why the increase in firm size?

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## What caused the increase in firm size?

**1. Globalization (larger Earnings):** General Motors sells worldwide

**3. Higher valuation multiples (larger Price / Earnings ratio)** for stocks and bonds, themselves due to:

- Lower interest rate  $r$  (savings glut?, demographics?)
- Lower risk premia (greater optimism about capitalism's resilience; the rich being less risk averse)?

**2. IT:** makes it easier to manage a very large firm

# Extension: Top $H$ executives

- Assume human cap increases firm value by factor:

$$1 + \sum_1^H C_h \times T_h \rightarrow \max S \times \left( 1 + \sum_1^H C_h \times T_h \right) - \sum_1^H w(T_h)$$

- Think of firm  $S_i$  as  $H$   $C_i$ -scaled assets each looking for manager :

$$(C_1 \times S_i, \dots, C_H \times S_i)$$

- In equilibrium, executive # $h$  at firm  $i$  earns:

$$w_{i,h} = D \times C_h^{1-\beta/\alpha} \times S_*^{\beta/\alpha} \times S_i(x)^{1-\beta/\alpha}$$

- Steepness of wage ratio and firm organization:  $\frac{w_1}{w_h} = \left( \frac{C_1}{C_h} \right)^{1-\beta/\alpha}$

# Rise in the supply of CEO talent: CEOs born in India

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CEO of Google 🇮🇳  
CEO of Microsoft 🇮🇳  
CEO of Adobe 🇮🇳  
CEO of Twitter 🇮🇳  
CEO of Mastercard 🇮🇳  
CEO of Pepsi 🇮🇳  
CEO of IBM 🇮🇳  
CEO of Albertsons 🇮🇳  
CEO of Micron 🇮🇳  
CEO of Netapp 🇮🇳  
CEO of Nokia 🇮🇳  
CEO of Palo Alto 🇮🇳  
CEO of Arista 🇮🇳  
CEO of Novartis 🇮🇳

Source: @stats\_feed, 8/26/22

# Extension: How wages fall when talent supply increases

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- Suppose that the talent supply of is multiplied by  $M$
- Then, for a given ranking  $n$ , pay falls by a factor  $M^\beta = M^{2/3}$
- So, if you double the talent supply, wages fall by 40%
- This increase in the talent supply (from India, MBAs etc) may explain the fact that US CEO pay has increased little since 2003
- It may also explain the relatively small rise before 1970 (increase in talent supply similar to Goldin-Katz)

# Extension: Model with incentives

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- Lots of people opine that incentives are a part of the story
- Is that true?
- Add incentives, both in theory and in calibrated empirics: work with Edmans, Landier, Sannikov, Sadzik (09, 11ab, 12):
- Findings
  - Incentives matter to set the optimal fraction of variable vs fixed pay
  - Incentives matter in the cross-section: If a firm is riskier, it needs to pay more
  - Incentives do not matter in the aggregate for the average level of pay: that's determined by productivity
  - ...if all firm are riskier, aggregate pay doesn't change

# Remark: Could a “stealing” model work?

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- Objection: wouldn't a “stealing” model work?
- Simplest model of stealing: a CEO in a firm of size  $S$  can extract a pay  $a S$ , for a coefficient  $a$
- But then, you violate Roberts' law,  $w(n) \sim S(n)^{1/3}$  : empirically, pay is less than proportional to size
- OK, imagine that we manage to contrive a reason why  $w(n) \sim S(n)^{1/3}$  . Then, you still don't get the time series right, i.e. don't get

$$w(n) = D \times S_{n^*}^{2/3} \times S_n^{1/3}$$

- So it seems very hard for stealing models to get the double scaling in the cross-section and time series



# Caveat: of course, CEOs are not perfect

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- There is a lot of extra richness:
- What do CEOs do? (Bloom et al, Bertrand Schoar 2003)
- There are interesting deviations from a perfect market
  - CEOs are overconfident (Malmendier and Tate 2005,8)
  - CFOs can be miscalibrated (Ben-David et al 2013)
  - Options are sticky in “number of shares” (Shue and Townsend 2017)
  - Talent is hard to identify (Tervio 2009)
  - Contagion effects might be strong (G. Landier 2008, Benabou Tirole 2016)
  - Wealth matters (Becker 2006, Edmans G. 2011)
- Still, the matching model, with a huge rise in size of stakes (6x), offers a useful 1<sup>st</sup> order point of departure

# Conclusion for CEOs

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## 1. **Simple CEO pay model.**

Under general assumptions:

$$w(n) = D \times S_{n^*}^{\kappa} \times S_n^{1-\kappa}$$

- “Reference firm” size,  $S^*$ , matters

## 2. **Empirical implications:** CEO compensation across *firms, time, countries, industries*

## 3. “Size of stakes” is the key driver. Probably, incentives, social norms, etc. matter much less (Kaplan Rauh 2013)

# Other superstars markets

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## **Other markets:**

- Top programmers: affect huge projects
- Top fund managers: affect large pools of money
- Top athletes: affect odds of winning, audience, value of ads
- Top actors: affect a lot the value of a movie
- Top lawyers: affect probability of success

## **Diffusion in market equilibrium:**

- Top works of art, real estate: wealthy people buy nice real estate, works of art, hire top divorce lawyers, surgeons etc
- So, diffusion of superstars economics across the whole economy

## **Non-stars:**

- Small stakes, no scope for scaling: nurses, school teachers, construction workers

# Policy?

- *If talent supply is inflexible: you could have ~~99% tax rate, nothing is distorted~~*
- *If talent supply is flexible: optimal taxes are low, or even negative, if talented people create growth theory-type externalities! (Jones '22)*
- The market tells us that we want more top programmers, surgeons, managers
  - So that people accumulate the right human capital, we should let the price signals work
  - Or if you tax them at rate  $T$ , subsidize education at rate  $T$
- Caveat: In some markets, private rewards may be  $>$  social rewards (e.g. hedge funds? Lockwood et al. 2017, Eeckhout et al. 2022), but in many markets (esp. with research, entrepreneurship), they're  $<$  social rewards.
  - Some very bad ideas: tax bonuses. Very bad, because it gives an incentives to give fixed rather than variable pay, and banks are less flexibility to cut costs in downturns

# Policy

## □ **On the elasticity of supply of talent:**

- 
- We don't know the *aggregate* elasticity of talent. So maybe a large, uniform income tax is OK?
  - The cross-sectional elasticity of talent (say, across US states) is pretty high (e.g. Akcigit et al. 2022)
  - So, if you're a country, you want to have lower taxes to attract talent, *ceteris paribus* (as US, UK)

## □ Overall, talents markets work well

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Two exceptions:

### 1. *The public sector*

- In Singapore, top public servants are highly educated, highly paid
- Probably underpaid / less qualified elsewhere
- Same for politicians: unimpressive, low quality offerings

### 2. *The discovery / nurturing of talent* may be suboptimal in many countries

- Countries spend resources fostering top athletes, not so much for other talents
- One could do the same for non-athletic talent: program for gifted children, exposure to innovation etc. (Bell et al. 2019)

# Conclusion

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- Sherwin Rosen (1981) was prescient
- Superstars economics very important in the past 50 years
  - In part due to rise in firm size, itself due to (i) lower interest rates and risk premium (ii) globalization (iii) IT
- We now have worked out models of superstars economics, including equilibrium wages, incentives, and empirical investigation
- Detailed studies of what CEOs do
- First order bottom line: This very high pay reflects the healthy functioning of talent markets.
- So, help the poor...
- .... But keep nurturing top talents, which are crucial for firm success, innovation, mankind's progress